

Methods

Bayesian change-point analyses in ecology

Brian Beckage¹, Lawrence Joseph², Patrick Belisle², David B. Wolfson³ and William J. Platt⁴

¹Department of Plant Biology, University of Vermont, Burlington, VT 05452, USA; ²Division of Clinical Epidemiology, McGill University Health Centre, Montreal, Quebec, Canada H3A 1A1; ³Department of Mathematics and Statistics, McGill University, Montreal, Quebec, Canada H3A 2K6; ⁴Department of Biological Sciences, Louisiana State University, Baton Rouge, LA 70803, USA

Author for correspondence:
 Brian Beckage
 Tel: +1 802 6560197
 Fax: +1 802 6560440
 Email: Brian.Beckage@uvm.edu

Received: 27 September 2006
 Accepted: 26 November 2006

Summary

- Ecological and biological processes can change from one state to another once a threshold has been crossed in space or time. Threshold responses to incremental changes in underlying variables can characterize diverse processes from climate change to the desertification of arid lands from overgrazing.
- Estimating the location of thresholds and ecological parameters in conjunction with thresholds can be difficult: ecological data are often 'noisy', which can make the identification of the locations of ecological thresholds challenging.
- Here, we illustrate this problem using two ecological examples and apply a class of statistical models well-suited to addressing this problem. We first consider the case of estimating allometric relationships between tree diameter and height when the trees have distinctly different growth modes across life-history stages. We next estimate the effects of canopy gaps and dense understory vegetation on tree recruitment in transects that transverse both canopy and gap conditions.
- The Bayesian change-point models that we present estimate both threshold locations and the slope or level of ecological quantities of interest, while incorporating uncertainty in the change-point location into these estimates. This class of models is suitable for problems with multiple thresholds and can account for spatial or temporal autocorrelation.

Key words: allometry, Bayesian, canopy gaps, change-point, climate change, *Pinus palustris*, recruitment, threshold

New Phytologist (2007) doi: 10.1111/j.1469-8137.2007.01991.x



© The Authors (2007). Journal compilation © *New Phytologist* (2007)

Introduction

Anthropogenic climate change is likely to transform many ecological communities over the next century. The mean global temperature has risen by *c.* 0.6°C over the past century, and the rate of warming since 1976 has been greater than any other period during the last 1000 yr (Mann *et al.*, 1998; Easterling *et al.*, 2000; IPCC, 2001). Anthropogenic climate change is likely to continue at the same or an accelerated rate for the foreseeable future (Hansen *et al.*, 2005; Meehl *et al.*, 2005), with global temperatures predicted to rise by another 1.4–5.8°C by the year 2100 (IPCC, 2001; Wigley, 2005).

Climate is an important determinant of species' ranges: rising temperatures associated with anthropogenic greenhouse gas emissions are predicted to lead to species migration poleward or upward in elevation (Krajick, 2004). Forest composition will shift as populations of some species decline and new species become established as regional climates respond to global warming. Climate-linked range shifts have already been observed in a variety of taxa (Walther *et al.*, 2002; Parmesan & Yohe, 2003).

Ecological systems may transition rapidly to altered states as climatic conditions cross critical thresholds, rather than slowly responding to changes in climate. Threshold responses

| | | | | | | | | | | | |
|---|----------------|---|---|--------------------------------|---|---|---|--------------------------|---|---------------------------|----------------------------|
|  | N | P | H | 1 | 9 | 9 | 1 | Operator: LinPing |  | Dispatch: 27.12.06 | PE: Natasha Stewart |
| Journal Name | Manuscript No. | | | Proofreader: Wu YanMing | | | | No. of Pages: 12 | Copy-editor: Andy Anderson | | |

are characteristic of diverse processes from climate change to the desertification of lands from overgrazing (van de Koppel *et al.*, 1997; Higgins *et al.*, 2002; Walker & Meyers, 2004). Threshold behaviors can result from nonlinear responses to incremental changes in underlying processes in which a gradual change in a process causes a disproportionate response once a critical threshold is reached (Maslin, 2004), such as might be caused by a positive feedback loop between an underlying drivers and the system response (Hoffman *et al.*, 2002; Crespi, 2004). Transitions between ecological states may also occur along spatial gradients in resource availability or disturbance frequency, for example. Similarly, patterns of growth or allocation within individuals can shift once a critical age or size has been reached (LaDeau & Clark, 2001). In these cases, the systems display a threshold response in which the system switches states once a boundary region has been crossed in the underlying driver (e.g. resource level or age of individual). In this paper, we distinguish two threshold responses: an abrupt change in a rate of a process (Fig. 1a) or a jump in the level of a process (Fig. 1b).

Estimating the location of thresholds in space or time and corresponding ecosystem responses (e.g. change in rate or level of an ecological process; e.g. Figure 1) can be a challenging problem that is likely to become increasingly important as ecosystems respond to anthropogenic climate change. The noisy nature of ecological data tends to obscure the identification of thresholds, introducing potentially large uncertainty

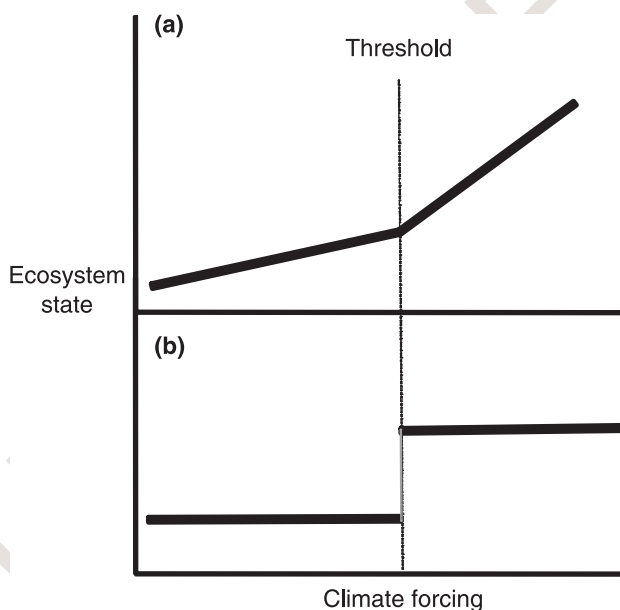


Fig. 1 Conceptual model of abrupt climate change. An abrupt change can occur in the rate (a) or level (b) of a process once a threshold is crossed. An abrupt change in both the rate and level of a process could also occur. We do not specifically consider this case, but the models we present could be easily generalized to this case.

into estimates of their location. The subsequent estimation of ecological quantities depends on the location of the underlying spatial or temporal threshold. A modeling approach is needed that simultaneously estimates the location of the threshold and the state of the system on either side of the threshold boundary, and that incorporates uncertainty in the threshold location into estimates of the state variables.

We illustrate this problem using two examples from our own research in forest dynamics and apply a class of models for addressing these challenges. In the first example, we estimate the allometric relationship between tree diameter and tree height in longleaf pine (*Pinus palustris* Mill.) for use in a forest simulation growth model. Longleaf pine shifts its allometric patterns as a function of life-history stage that produce distinctly different relationship between tree height and diameter as a function of tree size. Our objective is to estimate the relationship between tree diameter and height across life-history stages, which may necessitate estimating the location of change-points (i.e. thresholds, abrupt changes or discontinuities in this relationship). In the second example, we estimate tree seedling recruitment along a transect from closed canopy forest through gaps in the forest canopy created by the death of overstory trees. Light is often a limiting resource in forest understories (Canham, 1988; Pacala *et al.*, 1994) and its availability plays a central role in tree regeneration (Platt & Strong, 1989). Estimating changes in seeding densities associated with canopy and gap conditions requires identification of the transition from low to elevated light levels in the forest understory. The identification of this transition can be difficult in the absence of spatially extensive measurements of light levels because: (1) light gaps are offset towards the north in the northern hemisphere, with the degree of offset dependent on latitude, slope, and canopy height (Canham *et al.*, 1990); and (2) the canopies of bordering trees are irregular and change with time as they grow into the light gap (Valverde & Silvertown, 1997). Our objective is to estimate the locations of the canopy to gap transition in light levels, and corresponding levels of seedling recruitment of red maple (*Acer rubrum* L.) associated with gap and closed canopy conditions. In this example, the analysis is further complicated by consideration of spatial correlation between adjacent measurements of seedling recruitment. Spatial correlation in seedling counts in adjacent quadrats can result from patchy soils, local seed sources or other spatially variable processes that effect seedling establishment.

We address these estimation problems using a class of statistical models referred to as change-point models. We first use a simple change-point model to estimate the allometric relationship between tree height and diameter. We next employ a hierarchical change-point model to estimate the probable transitions from canopy to gap conditions with a hierarchical dependence between multiple transects and associated seedling densities in closed canopy and gap environments. Finally, we extend this model to allow for spatial

correlation between adjacent seedling counts. We fit these models using Bayesian methods.

Data and model description

Tree allometry

Platt *et al.* (1988) collected extensive data on the demography of longleaf pine in an old-growth stand in southern Georgia. The sampling of longleaf pine was stratified into two general size classes; stems with a diameter at breast height (d.b.h.) > 2 cm and stems with a d.b.h. < 2 cm. For the larger size class (referred to as 'trees' or 'adults'), a random sample of 399 individuals was selected across the 40 ha study site, and the height and d.b.h. of each sampled stem was recorded. Individual trees ranged up to 75.4 cm d.b.h and 244 yr of age. For the smaller size class, four 1-ha plots were randomly selected out of a total of 40 1-ha plots. All stems < 2 cm d.b.h. were censused in the four selected plots, resulting in a total of 222 juveniles. These juveniles consisted of individuals that had not yet reached breast height, *c.* 1.4 m, and so the diameter at the base and the height of their terminal bud were measured.

Our objective is to predict the height of longleaf pine trees as a function of their diameter. Previous studies have used power relationships or other nonlinear model forms to relate tree height to diameter and usually estimate model parameters through linear regression on log transformed scales (O'Brien *et al.*, 1995; Colbert *et al.*, 2002), but we model tree height using a linear model on untransformed tree height and diameter. While a single linear relationship is unlikely to be appropriate across life-history stages (e.g. seedling, sapling, adults), the relationship may be piecewise linear, resulting in over-restricted ranges of tree diameters where the transitions between these linear regions are change-points. Both the slope and the residual variance of the linear model are expected to vary among these different linear regions. Finally, we expect a discontinuity between the juvenile and adult size classes that reflects the offset introduced by measuring the diameter of these two size classes at different locations on the stem – juveniles are measured at their base while adults are measured at breast height. Our model must account for all these aspects of the data.

Model description Our change-point model is a piecewise linear regression with the transition points between adjacent linear regions unknown (Fig. 2). We allow for separate slopes and variances within each linear region, and estimate the offset introduced by measurement of stem diameter at different points on the stem. All parameters were estimated simultaneously using Bayesian methodology, allowing us to quantify both the uncertainty in the change point locations and the parameters defining the species abundance by means of probability distributions. In the Bayesian paradigm, before

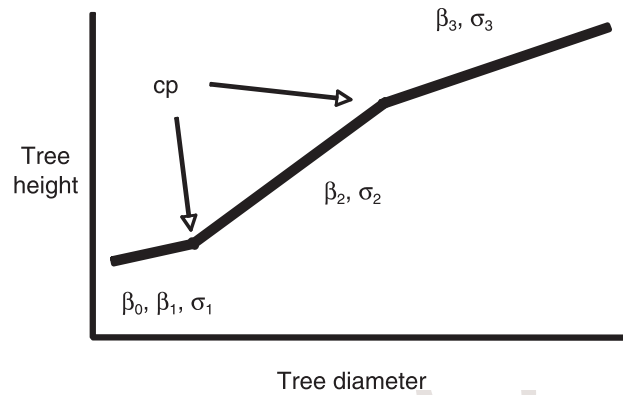


Fig. 2 Graphical illustration of our change-point model for tree allometry. The model is piecewise linear with the change-point (cp) locations defining the separate linear regions. We estimate a separate variance for each linear region. In addition, we estimate an 'offset' that represents the difference in stem diameter at the base and at breast height since stems were measured at alternative locations depending on stem height.

3

seeing the current data, our knowledge of the model parameters, including change-points, is described by a joint prior probability distribution. Once we have collected and modeled the current data through the change-point model's likelihood function, we revise our previous distributions to posterior distributions in light of this new information. These posterior distributions may then be used to make updated probability statements (i.e. inferences) about the parameters describing the species abundance as well as the change-point locations.

We modeled the height, h_i , of individual i as:

$\langle h_i | \mu_i, \tau_i \rangle \sim \text{Normal}(\mu_i, \tau_i)$ where μ_i is defined by the conditional:

if ($d_i < cp_1$ & $stem_i = \text{juvenile}$) then $\{\mu_i = \beta_0 + \beta_1 d_i\}$ +
 else if ($(dbh_i + k) < cp_1$ & $stem_i = \text{adult}$) then
 $\{\mu_i = \beta_0 + \beta_1 (dbh_i + k)\}$ +
 else if ($cp_1 < d_i < cp_2$ & $stem_i = \text{juvenile}$) then
 $\{\mu_i = \beta_0 + (\beta_1 - \beta_2)cp_1 + \beta_2 d_i\}$ +
 else if ($cp_1 < (dbh_i + k) < cp_2$ & $stem_i = \text{adult}$) then
 $\{\mu_i = \beta_0 + (\beta_1 - \beta_2)cp_1 + \beta_2 (dbh_i + k)\}$ +
 else if ($cp_2 < d_i$ & $stem_i = \text{juvenile}$) then
 $\{\mu_i = \beta_0 + (\beta_1 - \beta_2)cp_1 + (\beta_2 - \beta_3)cp_2 + \beta_3 d_i\}$ +
 else if ($cp_2 < (dbh_i + k)$ & $stem_i = \text{adult}$) then
 $\{\mu_i = \beta_0 + (\beta_1 - \beta_2)cp_1 + (\beta_2 - \beta_3)cp_2 + \beta_3 (dbh_i + k)\}$

(d_i is the diameter at the stem base; dbh_i is the stem diameter at breast height; k is the offset that converts diameter at breast height to basal diameter for adult data, cp_1 and cp_2 are the first and second change-points; and the β parameters are regression coefficients). The precision parameter τ_i , which is the inverse of variance, is given by the conditional:

if ($d_i < cp_1$ & $stem_i = juvenile$) then $\{\tau_1\}$
 else if ($(dbh_i + k) < cp_1$ & $stem_i = adult$) then $\{\tau_1\}$
 else if ($cp_1 < d_i < cp_2$ & $stem_i = juvenile$) then $\{\tau_2\}$
 else if ($cp_1 < (dbh_i + k) < cp_2$ & $stem_i = adult$) then $\{\tau_2\}$
 else if ($cp_2 < d_i$ & $stem_i = juvenile$) then $\{\tau_3\}$
 else if ($cp_2 < (dbh_i + k)$ & $stem_i = adult$) then $\{\tau_3\}$

The posterior distribution of the model parameters is proportional to

$$\begin{aligned} & P(\beta_0, \beta_1, \beta_2, \beta_3, cp_1, cp_2, k, \tau_1, \tau_2, \tau_3 | \mathbf{X}, \Theta) \propto \\ & P(\mathbf{X} | \beta_0, \beta_1, \beta_2, \beta_3, cp_1, cp_2, k, \tau_1, \tau_2, \tau_3) * \\ & P(\beta_0 | \mu_0, \tau_{\beta_0}^2) * P(\beta_1 | \mu_1, \tau_{\beta_1}^2) * P(\beta_2 | \mu_2, \tau_{\beta_2}^2) * P(\beta_3 | \mu_3, \tau_{\beta_3}^2) * \\ & P(\tau_1 | a_1, b_1) * P(\tau_2 | a_2, b_2) * P(\tau_3 | a_3, b_3) * \\ & P(cp_1 | a_{cp_1}, b_{cp_1}) * P(cp_2 | a_{cp_2}, b_{cp_2}) * P(k | m, n) \end{aligned} \quad (1)$$

where \mathbf{X} represents the observed data and Θ represents the prior parameter vector. The likelihood function is normal conditional on the mean and precision as indicated above. Bayesian analyses require a prior distribution over all unknown parameters. The parametric form of the prior probability distributions for the model components are:

$$\begin{aligned} & \langle \beta_j | \mu_j, \tau_{\beta_j}^2 \rangle \sim \text{Normal}(\mu_j, \tau_{\beta_j}^2); \\ & \langle \tau_{\beta_j} | a_j, b_j \rangle \sim \text{Gamma}(a_j, b_j) \\ & \langle cp_i | a_i^{cp}, b_i^{cp} \rangle \sim \text{Gamma}(a_i^{cp}, b_i^{cp}); \\ & \langle k | m, n \rangle \sim \text{uniform}(m, n) \end{aligned}$$

The form of these prior probability distributions was chosen both to facilitate computations and to represent beliefs regarding model parameters. Our general strategy was to employ diffuse or noninformative prior distributions, so that final inferences will depend solely or almost solely on the data. The exception to this was the uniform prior on k , which was constrained to lie between -1 and 5 (cm). The prior parameter vector that we used, and that was assigned a priori, was:

$$\begin{aligned} & (\mu_j, \tau_{\beta_j}^2, a_j, b_j, a_i^{cp}, b_i^{cp}, a_2^{cp}, b_2^{cp}, m, n) = \\ & (0, 0.01, 0.001, 0.001, 0.003, 0.001, 0.0015, 0.0001, -1.5) \end{aligned}$$

The normal prior on the β_j coefficients, for example, is centered at 0 with a small precision (equivalent to a large variance), which allows the β_j s to be primarily determined by the data. Nevertheless, it is sometimes possible that even 'noninformative' prior distributions will have some influence on the posterior distributions, so that the sensitivity of the model to the priors is assessed. We varied both the form of the prior distributions (for example, replacing the gamma priors on cp_1 and cp_2 with uniform priors over the range (0,80)) as well as the parameterization of the prior distributions to assess

model sensitivity. Our inferences were insensitive to variation in our diffuse priors. Of course, the priors may be selected to reflect results from previous studies or one's knowledge of the system and be allowed to drive the inference to a greater degree than in the current analysis.

While expression (1) above is proportional to the posterior distribution of the model parameters, normalizing the posterior distribution requires integration of the expression over its entire parameter space. Although this is intractable, an alternative approach is to simulate a large number of random samples from the posterior distribution of model parameters, represented by a vector Θ , and to use these random samples to make inferences about Θ . We did this using Markov Chain Monte Carlo (MCMC) methods (Gelman *et al.*, 2003). With a large number of vectors of Θ , drawn from the joint posterior distribution of Θ , we can abstract any component parameter of interest and use the large number of simulated values to approximate the marginal posterior distribution of the parameter. We programmed our MCMC sampler in the open source language R and the code is available from the author.

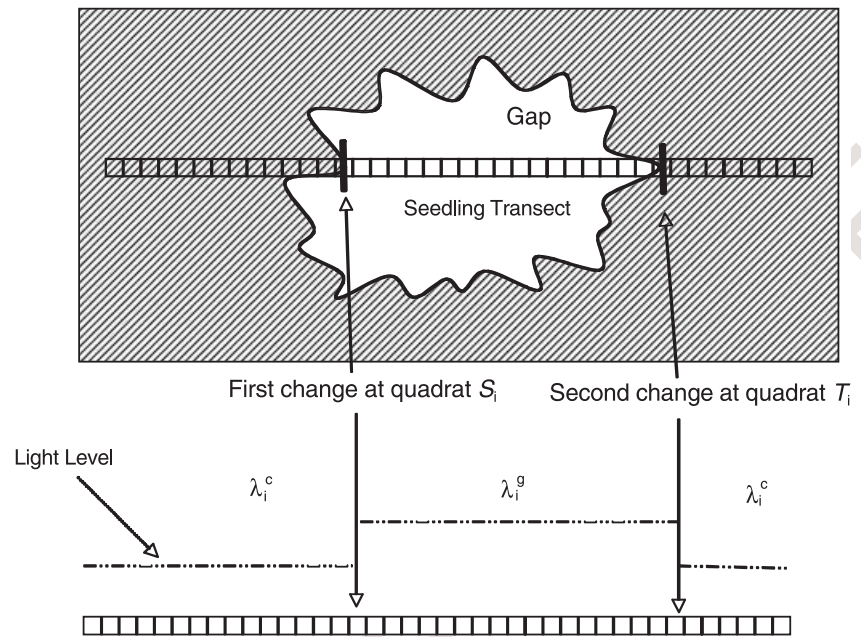
Seedling recruitment

Beckage *et al.* (2000) studied tree recruitment with respect to canopy gaps and presence of the understory shrub *Rhododendron maximum* L. The research was conducted in mixed-oak forests at the Coweeta Hydrologic Laboratory located near Franklin, NC, USA (in the Southern Appalachians). The mixed oak forests are dominated by *Quercus prinus* L., *Quercus coccinea* Muenchh., *Quercus rubra* L., and *Quercus velutina* Lam., but *Acer rubrum* dominates the seedling bank. Much of the forest understory is dominated by *R. maximum*, an ericaceous, evergreen shrub that occurs at all elevations in the Coweeta basin (Swank & Crossley, 1988). *Rhododendron* forms a dense subcanopy layer 3–7 m in height. Stem densities range from 5000 to 17 000 ha⁻¹ (Baker & van Lear, 1998) and leaf area indices (LAI) range from approximately 4.8 to 6.6. Stem densities in our plots were approx. 8900 ha⁻¹ with diameters most frequently ranging from 4 to 7 cm d.b.h., but sometimes > 10 cm d.b.h.

Beckage *et al.* (2000) created a series of 12 artificial gaps under two understory conditions: half of the plots had a dense *Rhododendron* understory, while the remaining plots lacked *Rhododendron*. *Rhododendron* has a patchy distribution at these sites, permitting experimental gaps (with and without *Rhododendron*) to be located in close proximity, thus allowing for consistent overstory composition, slope, soils and microclimate. Up to five canopy trees were girdled to create each gap. Gaps were approx. 20 m in diameter (for expanded gap definition see Runkle, 1981) with standing dead trees and, thus, resulted in minimal disturbance to the understory.

A transect comprised of 40 contiguous 1-m² quadrats was established across each planned gap before its creation. Transects included 20 central quadrats spanning the diameter

Fig. 3 (a) Layout of a typical experimental gap. The long axis of the transect was oriented in a north–south direction. The experimental gaps were designed so that the central 20 quadrats should subtend the canopy opening but the irregular shapes of the surrounding canopies make this unlikely. (b) The change-point model for a single transect. The first change-point occurs at quadrat S_i for transect i while the second change occurs at quadrat T_i . λ_i^c is the rate parameter of a Poisson distribution describing the seedling counts in canopy conditions while λ_i^g describes the rates in gap conditions.



of the gap and 20 outer quadrats beneath the surrounding canopy. However, the border between gap and canopy conditions is irregular, reflecting the canopy shapes of bordering trees so that all 20 central quadrats might not subtend the canopy gap (Fig. 3). Consistency of transect orientation is an important consideration in the present analysis because elevated light levels, offset toward the north side of canopy gaps in the northern hemisphere (Canham *et al.*, 1990), affect the expected distribution of change-point locations. Seven of the 12 transects were oriented in a general north–south direction and these were the focus of our analysis. Only three of these transects contained *Rhododendron* in their understory. Beckage *et al.* (2000) conducted annual surveys of tree seedlings in the transects in mid to late summer. Recruits that germinated in the year in which the census was conducted (i.e. seedlings) were distinguished from older recruits by the presence of cotyledons and a lack of terminal bud scale scars. *Acer rubrum* was the only species with abundant seedlings that was widely distributed across transects. In the current analysis, we focus on seedlings of *A. rubrum* that occurred in the seven transects, identified above, in a single year (1997).

Model description The Bayesian change-point model for seedling counts has two components: a model describing seedling abundance and a model describing change-point locations. The seedling model is a hierarchical Bayesian model, so that similar transects or portions of transects (e.g. with *Rhododendron*, gap conditions, etc.) were united by higher levels of the model. This is the Bayesian analogue to classical random effects models.

The hierarchical model can be described in three stages or levels. We represent the seedling counts in quadrats by a

vector $X_{i,j}$, with subscript i designating the transect and j representing the quadrat within transect i . At the first level of the hierarchy, seedling counts in transect i are assumed to be independent and to follow Poisson distributions with respective rate parameters λ_i^g and λ_i^c depending on whether the portion of the transect occurs under gap or canopy conditions (Fig. 3). The second level of the hierarchy links the λ_i s for similar conditions (e.g. gap vs canopy and *Rhododendron* vs non-*Rhododendron* in a given year) across transects and assumes that the λ_i s follow a Gamma distribution. We choose the Gamma distribution because it is commonly used to represent variability in the means of Poisson random variates. This level allows for the ‘borrowing of strength’ or the use of information from separate sampling units at a lower level in the hierarchy to estimate a higher level parameter that spans across sampling units, which is an important advantage of hierarchical models. While individual quadrats are independent Poisson variates, the means of these Poisson variables are assumed to be similar, but not identical, across transects. In general, if only a small amount of data is available for a particular $X_{i,j}$, then the parameter value for the mean level in the gap or canopy portion of the transect will be close to the mean level of the other similar transects, there being little evidence to the contrary. Conversely, if many data are available, the estimated mean will be close to the mean of the data. With moderate amounts of data, the estimated mean will be a data-based compromise between the observed mean level and the overall mean levels of all similar transects. At the top level of the hierarchy, the b^{-1} parameter of the Gamma distribution is itself distributed as an Inverse Gamma. The hierarchical random effects model structure allows global inferences to be made on the two recruitment rate parameters for similar transects while

still allowing for individual transect parameters to vary. Within groups of similar transects, inferences are made through lambda stars, λ^* s, which are the expected value of a randomly selected lambda in that treatment combination group. Our seedling model is then

$$\begin{aligned} \langle X_g^i | \lambda_g^i \rangle &\sim \text{Poisson}(\lambda_g^i) & \langle X_c^i | \lambda_c^i \rangle &\sim \text{Poisson}(\lambda_c^i) \\ \langle \lambda_g^i | a_g, b_g^{-1} \rangle &\sim \text{Gamma}(a_g, b_g^{-1}) \\ \langle \lambda_c^i | a_c, b_c^{-1} \rangle &\sim \text{Gamma}(a_c, b_c^{-1}) \\ \langle b_g^{-1} | \gamma_g, \zeta_g \rangle &\sim \text{Inverse Gamma}(\gamma_g, \zeta_g) \\ \langle b_c^{-1} | \gamma_c, \zeta_c \rangle &\sim \text{Inverse Gamma}(\gamma_c, \zeta_c) \end{aligned}$$

where the subscripts g or c indicate gap or canopy conditions, respectively.

The parameters α_c , α_g , γ_c , γ_g , ζ_c , and ζ_g were assigned values a priori and determined the prior distributions of the seedling portion of the model. We used the same priors for both canopy and gap portions of transects allowing the prior parameter vector to be written as $\theta_p = (\alpha, \gamma, \zeta)$. Our set, θ_p , of prior parameters was (1.05, 0.01, 0.01). We explored the sensitivity of our inferences using two other prior sets: alternative prior set 1 (1.0, 0.01, 0.01) and alternative prior set 2 (12.0, 0.5, 0.5). The prior specification was diffuse for all three prior sets, enabling the current data to play a dominant role in the final inference (i.e. the posterior predominately reflects the data with the prior exerting little influence). In fact, the prior sets carry the equivalent weight of 0.05, 0 and 11 seedlings, respectively. In the present case, the results from the three prior sets were very similar, indicating that they had little influence on the posterior distribution.

We modeled each transect as having two change-points. In transect i , the first change-point occurs in quadrat S_i and represents the unknown point where canopy conditions end and gap conditions begin (Fig. 3). Similarly, T_i is the quadrat where the second change-point occurs and represents the transition back from gap to canopy conditions. S_i was modeled as following a multinomial distribution ($p_{sj}, j = 1 \dots 20$) where p_{sj} is the probability of the change occurring in quadrat j . The prior probabilities for the vector p_s were given a Dirichlet ($a_{sj}, j = 1 \dots 20$) distribution: the Dirichlet distribution is conjugated to the multinomial distribution, which facilitates computation of the posterior distribution (Gelman *et al.*, 2003). The second change-point, T_i , was modeled in a similar manner. We set, a priori, the components of the vectors a_s and a_t to 1/200 so that these priors were diffuse; their influence on the posterior distribution was equivalent to only 1/10 of a transect. It is apparent from our model description that we have constrained the first change-point to occur in the first half of each transect and the second change point to occur in the second half of the transect. Furthermore, we have, a priori, said that the change-point is equally likely to occur in any quadrat within this region. The change point of our model is given by

$$\begin{aligned} \langle S^i | p_j, j = 1 \dots 20 \rangle &\sim \text{Multinomial}(n, p_j, j = 1 \dots 20) \\ \langle T^i | p'_j, j = 21 \dots 40 \rangle &\sim \text{Multinomial}(n, p'_j, j = 21 \dots 40) \\ \langle p_j | a_j, j = 1 \dots 20 \rangle &\sim \text{Dirichlet}(a_j, j = 1 \dots 20) \\ \langle p'_j | a'_j, j = 21 \dots 40 \rangle &\sim \text{Dirichlet}(a'_j, j = 21 \dots 40) \end{aligned}$$

(S^i and T^i refer to the first and second change-points in transect i ; a_j and a'_j are the Dirichlet priors on the probabilities, p and p' , of the multinomial distribution for the first and second change-points).

We combined the Poisson and multinomial portions of our model to estimate the posterior distribution of all model parameters. The posterior distribution is proportional to

$$\begin{aligned} P(\lambda_{ci}, \lambda_{gi}, a_c, b_c, a_g, b_g, S_i, a_j, p_j, T_i, p'_j, a'_j | X_*) &\propto \\ P(X_* | \lambda_{ci}, \lambda_{gi}, S_i, T_i) &* P(\lambda_{ci} | a_c, b_c) * P(a_c) * \\ P(b_c | \gamma_c, \zeta_c) * P(\gamma_c) * P(\zeta_c) &* P(\lambda_{gi} | a_g, b_g) * P(a_g) * \\ P(b_g | \gamma_g, \zeta_g) * P(\gamma_g) * P(\zeta_g) &* P(S_i | p_j) * P(p_j | a_j) * \\ P(a'_j) * P(T_i | p'_j) * P(p'_j | a'_j) &* P(a'_j) \end{aligned}$$

We again estimated model parameters using MCMC, but in this case we sampled the posterior distribution using the freely distributed WINBUGS software that generates samples from the posterior distribution of a user-specified model (Spiegelhalter *et al.*, 1995, <http://www.mrc-bsu.cam.ac.uk/bugs>).

Spatial correlation The model in the preceding section assumes conditional independence between adjacent quadrats within each transect. This assumption may be reasonable, since, given the mean values that apply to a pair of adjacent quadrats, the actual seedling recruitment within each quadrat may be independent from neighboring quadrats. Nevertheless, it is also possible that, for example, soils are more similar in adjacent areas within a transect compared with quadrats further away, so that some correlations may appear across adjacent quadrats, even given the overall mean level. Therefore, we extended our model to account for potential correlation in adjacent quadrats. The change-point model remains identical to that above, but we now allow correlations between seedling counts in adjacent quadrats by including a Gaussian Markov random field (GMRF) prior for random effects on the λ across quadrats within a transect (Besag & Kooperberg, 1995; Besag & Higdon, 1999).

We modified the structure of the seedling model to incorporate the GMRF prior by incorporating a linear model for treatment effects that allowed for modeling of spatial effects, i.e. the z_j^i s, of being in quadrat j :

$$\begin{aligned} \langle X^i | \lambda^i \rangle &\sim \text{Poisson}(\lambda^i) \\ \log(\lambda^i) &= \mathbf{Y}\boldsymbol{\beta} + z_j^i \\ \langle \beta_0 | \tau_0 \rangle &\sim \text{Normal}(0, \tau_0) & \langle \tau_0 | a_0, b_0 \rangle &\sim \text{Gamma}(a_0, b_0) \\ \langle \beta_c | \tau_c \rangle &\sim \text{Normal}(0, \tau_c) & \langle \beta_g | \tau_g \rangle &\sim \text{Normal}(0, \tau_g) \end{aligned}$$

(\mathbf{Y} is the design matrix that codes for gap and canopy conditions as well as for transects; $\mathbf{\beta}$ is the vector of regression parameters describing canopy, gap and transect effects). The transect effect is assumed to be random with mean 0 and precision τ_0 , where τ_0 has a Gamma prior distribution (a hierarchical model structure). Our design matrix is not full rank but is nevertheless estimable using Bayesian methods. The prior vectors were given values of $(a_0, b_0) = (0.1, 0.1)$ and $(\tau_c, \tau_g) = (1.0 \times 10^{-5}, 1.0 \times 10^{-5})$. We placed a locally linear GMRF prior on z_j^i :

$$\langle z_j^i | z_{dj}^i \rangle \sim \text{Normal} \left(z_{dj}^i, \frac{\tau_z^i}{n_j} \right) \quad \text{where} \quad z_{dj}^i = z_{j-1}^i + z_{j+1}^i$$

where the spatial effect of being in quadrat j depends on only quadrats immediately adjacent to the focal quadrat j . The spatial effects (z_s) model spatially structured residual variance in seedling abundance that remains after the main effects (e.g. gaps, *Rhododendron*, transects) have been estimated. The prior on the precision parameter τ_z^i is

$$\langle \tau_z^i | a_z, b_z \rangle \sim \text{Gamma}(a_z, b_z)$$

with $(a_z, b_z) = (0.001, 0.001)$. The diffuse specification of the prior on means that its estimated value will be primarily determined by the data. We fit this spatial model using the 'car.normal' functionality within the GeoBUGS module of WINBUGS.

Results

Tree allometry

Our two change-point model fitted the observed data well, with the regression line and change-point locations bisecting the cloud of observed data points (Fig. 4b). The discontinuity created by the diameter measurements being taken alternatively at the stem base or breast height has been accounted for through estimation of an offset (i.e. ' k ' in Table 1): The data points in Fig. 4b have been adjusted by k . The estimates of variance among the three change-point regions were very different, confirming the need to allow for separate variances (Table 1). Summary statistics for all model parameter estimates are presented in Table 1. We also fitted a three change-point model to these data but there was no strong support for a third change-point, as shown by a flat likelihood and subsequent strong correlation between change-point locations and k in this model.

Seedling recruitment

Our models captured the observed variability in seedling counts across transects (Figs 5 and 6). Three of the four

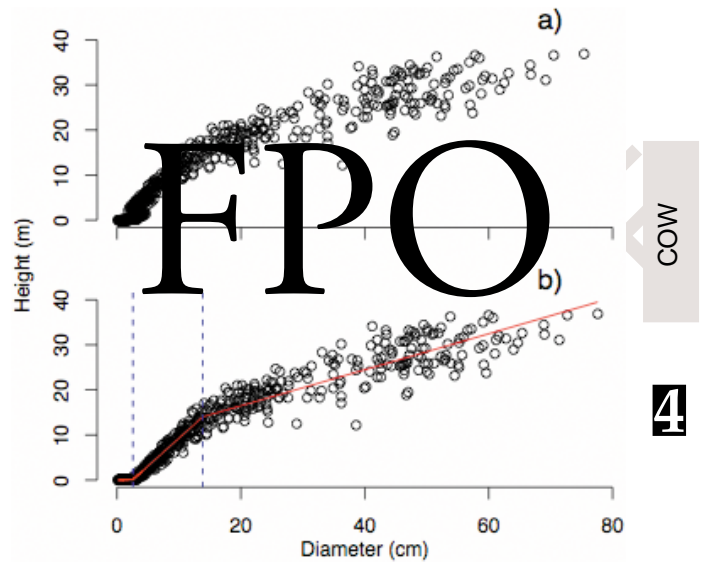


Fig. 4 Allometry of longleaf pine in an old growth forest. (a) Heights and diameters of individual trees. Stem diameter is measured at the base for stems < 1.4 m in height and at 1.4 m for all other stems. Note the discontinuity this imposes on the plots of raw data. (b) Model fit with location of change-points (vertical dotted lines) and estimated tree height (solid line). Note that the discontinuity has been adjusted for in the model fit (data points have been adjusted by the estimated parameter ' k ' that estimates the difference in diameter between stem base and breast height).

Table 1 Parameter estimates for the two change-point model of tree allometry

| Parameter | Quantile | | |
|--------------|----------|----------|----------|
| | Mean | 0.025 | 0.975 |
| β_0 | -0.0169 | -0.0257 | -0.00803 |
| β_1 | 0.0553 | 0.0493 | 0.0612 |
| β_2 | 1.23 | 1.11 | 1.35 |
| β_3 | 0.399 | 0.337 | 0.444 |
| k | 2.20 | 1.79 | 2.75 |
| cp_1 | 2.58 | 2.52 | 2.61 |
| cp_2 | 13.8 | 11.7 | 17.5 |
| σ_1^2 | 0.000552 | 0.000442 | 0.000688 |
| σ_2^2 | 1.15 | 0.793 | 1.59 |
| σ_3^2 | 11.5 | 9.51 | 13.9 |

Estimates are based on 40 000 samples following a burn in of 10 000 samples. 'Burn in' is the practice of discarding early Markov Chain Monte Carlo (MCMC) iterations to allow convergence to the target distribution before using samples to learn about model parameters (Gelman *et al.*, 2003). Although our model was parameterized in terms of precisions (inverse of variance), we report results in terms of variances for ease of interpretation.

non*Rhododendron* transects showed evidence of a strong gap effect (e.g. higher recruitment rates in the center portion of the transect) with a much weaker effect in the remaining transect (Fig. 5). All three of the *Rhododendron* transects

COW

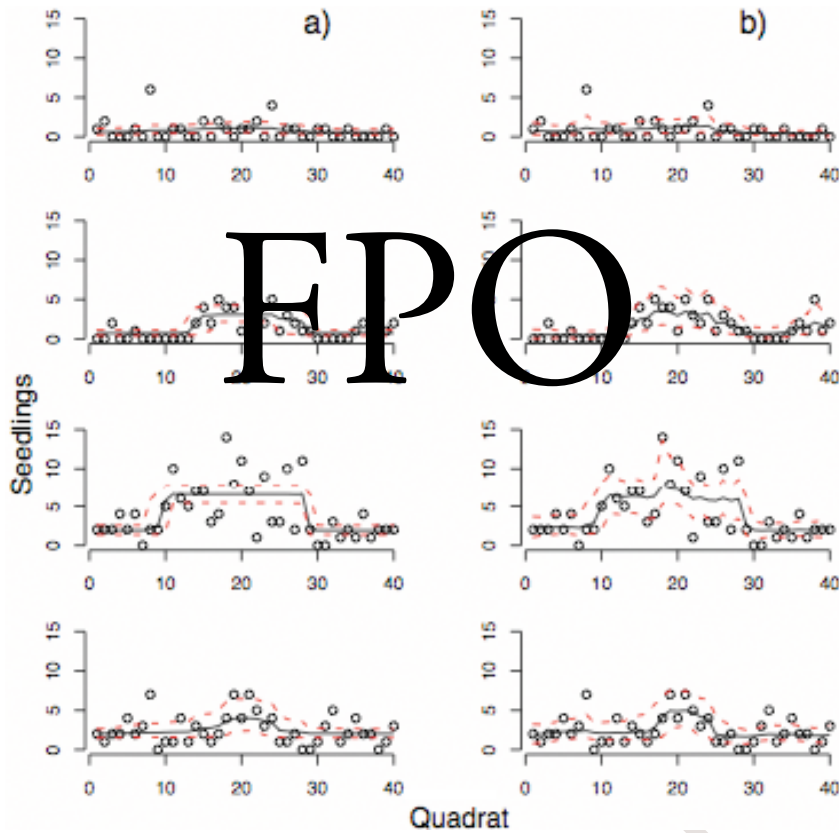


Fig. 5 The mean λ s or 'seedling recruitment rates' (solid lines) along with 95% credible interval (broken lines) for each quadrat (1–40) in the four transects that lack *Rhododendron*. The four transects are displayed in separate vertical panels. The open circles represent the observed seedling counts. The left column (a) display results for the nonspatial model while the right column (b) displays results for the spatial model.

COW

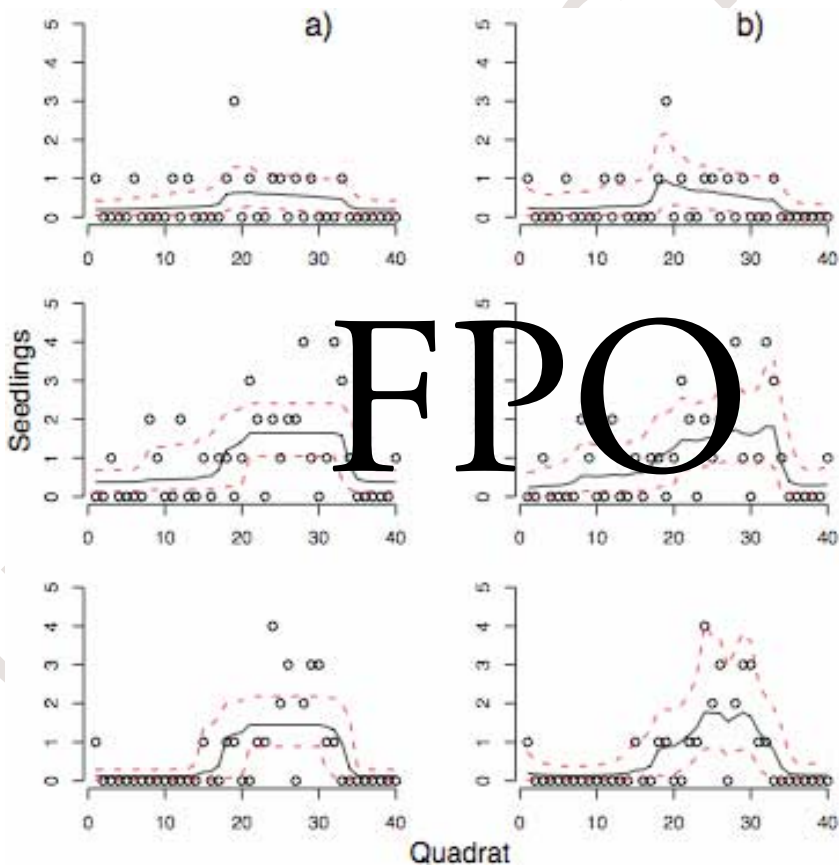


Fig. 6 The mean λ s or 'seedling recruitment rates' (solid lines) along with 95% credible interval (broken lines) for each quadrat (1–40) in three transects with *Rhododendron*. The three transects are displayed in separate vertical panels. The left column (a) display results for the non-spatial model while the right column (b) displays results for the spatial model.

similarly had higher recruitment rates in the central region of the transect where the gap was located (Fig. 6). The region of elevated seedling density was offset to the north in the *Rhododendron* transects, as expected in the northern hemisphere. The seedling model that included spatial correlation captured much of the local variation in seedling density within transects outside of the main gap-canopy effects (Figs 5b and 6b).

The expected seedling recruitment rate λ^* was greater in gaps compared with closed canopy conditions, with a probability between 0.92 and 1.00 depending on model and *Rhododendron* presence (Table 2). The spatial model resulted in a higher probability of a gap effect than the nonspatial model: 0.99 compared with 0.92, and 0.97 compared with 1.00 for non*Rhododendron* and *Rhododendron* conditions, respectively (Table 2). The number of seedlings was 2.8 times greater in gaps without *Rhododendron* compared with adjacent canopy, but 5.4–7.4 times greater in gaps with *Rhododendron*. Despite the larger gap effect with *Rhododendron*, seedling density was greater without *Rhododendron* by a factor of 2.6 (gap conditions) to 5.1 (canopy conditions). Seedling density was greater without *Rhododendron* regardless of canopy condition with probabilities ranging from 0.90 to 0.98 (Table 2).

Our estimates of seedling recruitment rate integrated across the uncertainty in change-point locations (Fig. 7). The change-point locations were better defined in the *Rhododendron* compared with the non*Rhododendron* transects (Fig. 7a,c vs 7b,d). Most of the probability was distributed in narrow regions for both the first and second change-points in the *Rhododendron* plots but was more diffusely distributed in the non*Rhododendron* plots. This result is consistent with the larger gap effect estimated in the *Rhododendron* plots (Table 2).

Discussion

Change-point models provide a methodology for concurrently estimating the location of thresholds in ecological or

biological processes and estimating parameters that describe that process on either side of the threshold. We were able to incorporate the uncertainty in our change-point locations into estimates of parameters of interest (e.g. slopes and variance of an allometric relationship, and recruitment rates of seedlings). We anticipate that this methodology will be particularly appropriate for modeling ecological responses to current and past global climate change. Anthropogenic forcing of the climate system is increasingly expected to result in large nonlinear system responses as thresholds are crossed (CACC, 2002): increasing evidence suggests that ecological systems will display similar threshold responses (Higgins *et al.*, 2002; Maslin, 2004). The change-point methodology presented here provides a technique for modeling these threshold processes.

Tree allometry

Our two change-point model captured the relationship between tree height and diameter for longleaf pine (Fig. 4b). We believe that the piecewise linear formulation of our change-point model is a biologically appropriate model for this process since the change-points reflect significant life-history events in longleaf pine. The first change-point, for example, represents the transition from the ‘grass’ stage during which longleaf pine juveniles experience growth in stem diameter and in their root system but little growth in stem height. This is an adaptation to frequent fires: the juveniles have dense tufts of needles (superficially resembling a grass clump) that protect their apical meristems from fire damage until they have stored sufficient energy reserves for rapid height growth. This ‘bolting’ strategy safely removes the apical meristem from the region in the understory where fire damage is most likely (Platt *et al.*, 1988; Platt & Rathbun, 1993). The second change-point reflects the entry of the longleaf into the canopy, after which height growth slows with respect to diameter growth. Once the stem transitions into the canopy, height growth is less important as competition for light is

Table 2 Results for seedling counts in gap and canopy conditions in the presence or absence of the understory shrub *Rhododendron*

| | Non <i>Rhododendron</i> (R^-) | | <i>Rhododendron</i> (R^+) | |
|--------------------------------|-----------------------------------|------------------|-------------------------------|------------------|
| | Nonspatial model | Spatial model | Nonspatial model | Spatial model |
| $P(\lambda_g^* > \lambda_c^*)$ | 0.92 | 0.99 | 0.97 | 1.00 |
| λ_g^* | 4.82 (1.65,12.9) | – | 1.83 (0.50,5.89) | – |
| λ_c^* | 1.73 (0.60,4.69) | – | 0.34 (0.08,1.13) | – |
| Multiplicative factor | – | 2.84 (1.68,4.11) | – | 7.45 (2.48,21.5) |
| $P(R^- > R^+)$ | Canopy 0.98 | 0.97 | Gap 0.90 | 0.91 |

λ_g^* and λ_c^* refer to the expected recruitment rate of seedlings in gap or closed canopy conditions, while R^- and R^+ refer to the absence or presence of *Rhododendron*, respectively. The estimates presented are means while the values in the parentheses given the 95% credible intervals, based on 40 000 samples following a burn in of 10 000 samples. The ‘Multiplicative Factor’ represents the factor by which the number of seedlings found in quadrats is increased in gap relative to closed canopy conditions.

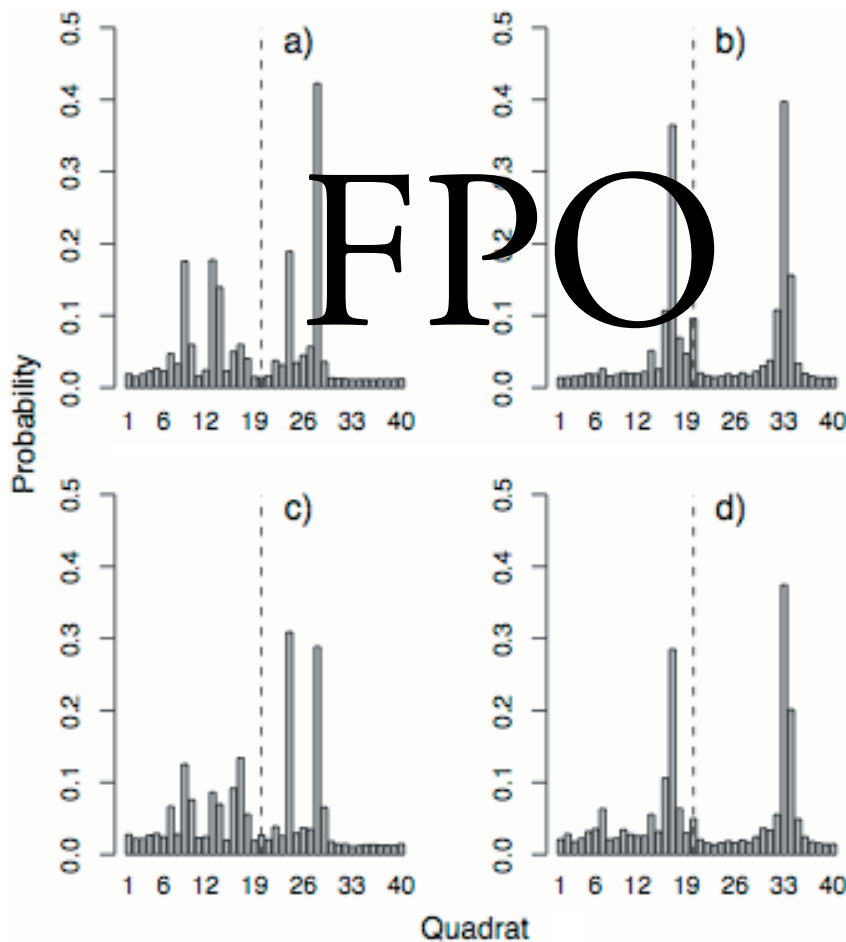


Fig. 7 The probable locations of the first and second change-points for new seedlings along transects for first-year seedlings in 1997 estimate for (a) non*Rhododendron* plots using nonspatial model, (b) *Rhododendron* plots using nonspatial model, (c) non*Rhododendron* plots using spatial model and (d) *Rhododendron* plots using spatial model. The first change-point is constrained to occur in the first half of each transect (left of dotted line) while the second change-point must occur in the second half of the transect. The height of the bars represents the probability of the change point occurring in a given quadrat.

reduced (i.e. the stem has captured a region of the canopy with unrestricted exposure to sunlight). We note that inspection of Fig. 4b suggests that an additional change-point may be justified in the diameter range of 60–70 cm, where height growth appears to cease (perhaps as a result of recurrent hurricane damage; Platt & Rathbun, 1993). There are currently insufficient data to support definitively calling this a change-point: the likelihood is flat and a third change-point tends to be placed at smaller diameters. One advantage of Bayesian methods is that we can use our own (or expert) judgment to place a strong prior distribution on the location of the change-point in the region of 60–70 cm, forcing a change-point in this region.

Seedling recruitment

Our change-point analysis found strong evidence for an effect of both gaps and *Rhododendron* on seedling recruitment. The density of seedlings was greater in gaps compared with closed canopy regardless of the presence of *Rhododendron* (Table 2). Seedling density was greater in areas outside of *Rhododendron*

in both gap and canopy conditions compared with areas lacking the shrub (Table 2). The change-point locations were more clearly identified in the *Rhododendron* transects than in transects without *Rhododendron* (Fig. 7), which was consistent with a stronger gap effect, relative to canopy conditions, within *Rhododendron* transects (Table 2). Light levels are generally much lower beneath *Rhododendron* than in forests lacking the shrub (Beckage *et al.*, 2000); our results suggest that even modest increases in light levels associated with small overstory gaps can increase seedling recruitment under very low light conditions, such as occur beneath *Rhododendron*. The more equivocal identification of the change-point locations in areas without *Rhododendron* may be because background light levels beneath the intact canopy in areas lacking *Rhododendron* were relatively high (Beckage *et al.*, 2000), which would tend to obscure the gap/canopy boundary when the gap effect on light levels is not large. Our canopy gaps produced only modest increases in light levels because of their relatively small size and because of the presence of standing dead trees, which would tend to reduce increases in insolation (Beckage *et al.*, 2000).

Bayesian models

We fit out change-point models using Bayesian methodology because of advantages associated with the Bayesian compared with conventional approaches. The Bayesian analysis easily allows inclusion of information from previous studies through the prior distribution (Gelman *et al.*, 2003). This provides a simple way of building on the results of previous work rather than basing all inferences on the current data only. Furthermore, while some change-point models are estimable using classical statistical methodology, extending these methods to more complex problems that are hierarchical or that incorporate spatial autocorrelation can be problematic. Bayesian methods can easily accommodate a large class of complex models (Clark, 2005). Finally, the types of inferences available from Bayesian models are better able to address questions of direct scientific interest (Ellison, 2004). The results of Bayesian analyses are straightforward to interpret (i.e. they are probability statements about model parameters conditional on the data and any available prior information, which is not the case in classical statistics).

Change-points models have been used extensively in the statistical literature, but have not been commonly used in ecology. Edge detection methods have been used by ecologists to identify regions of rapid change; this is a similar objective to change-point analyses (Fortin & Drapeau, 1995). Ver Hoef (1996) presented a change-point model for vertical cover in a single transect through a grassland, and fitted the model using an empirical Bayes procedure. The methodology used here differs from this application in several aspects. Our transect model accommodates multiple transects by combining them into several similar groups and using a hierarchical model to combine information from across groups. Our Bayesian approach also avoids the practice of using the current data to estimate parameters of the prior distribution, advocated in empirical Bayes methods, but generally not accepted by Bayesians (Ver Hoef, 1996). Finally, we explicitly model spatial dependence between adjacent quadrats: these methods could also be used to model temporal dependence in time series data.

Acknowledgements

We thank Jay Ver Hoef for his insightful comments on an earlier version of this manuscript. This paper was prepared as a contribution to an Ecological Society of America Symposium on 'Mucking through multifactor experiments: design and analysis of multifactor studies in global change research' in Memphis, Tennessee, USA.

References

Baker TT, van Lear DH. 1998. Relations between density of rhododendron thickets and diversity of riparian forests. *Forest Ecology and Management* 109: 21–32.

- Beckage B, Clark JS, Clinton B, Haines B. 2000. A long-term study of tree seedling recruitment in Southern Appalachian forests: the effects of canopy gaps and shrub understories. *Canadian Journal of Forest Research* 30: 1617–1631.
- Besag J, Higdon D. 1999. Bayesian analysis of agricultural field experiments (with discussion). *Journal of Royal Statistical Society, Series B* 61: 691–746.
- Besag J, Kooperberg CL. 1995. On conditional and intrinsic autoregressions. *Biometrika* 82: 733–746.
- CACC (Committee on Abrupt Climate Change). 2002. *Abrupt climate change: inevitable surprises*. Washington, DC, USA: National Academy Press.
- Canham CD. 1988. Growth and canopy architecture of shade tolerant trees: the response of *Acer saccharum* and *Fagus grandifolia* to canopy gaps. *Ecology* 69: 786–795.
- Canham CD, Denslow JS, Platt WJ, Runkle JR, Spies TA, White PS. 1990. Light regimes beneath closed canopies and tree-fall gaps in temperate and tropical forests. *Canadian Journal of Forest Research* 20: 620–631.
- Clark JS. 2005. Why environmental scientists are becoming Bayesians. *Ecology Letters* 8: 2–14.
- Colbert KC, Larsen DR, Lootens JR. 2002. Height diameter equations for thirteen Midwestern bottomland hardwood species. *Northern Journal of Applied Forestry* 19: 171–176.
- Crespi BJ. 2004. Vicious circles: positive feedback in major evolutionary and ecological transitions. *Trends in Ecology and Evolution* 19: 627–633.
- Easterling DR, Karl TR, Gallo KP, Robinson DA, Trenberth KE, Dai A. 2000. Observed climate variability and change of relevance to the biosphere. *Journal of Geophysical Research-Atmospheres* 105: 20101–20114.
- Ellison AM. 2004. Bayesian inference in ecology. *Ecology Letters* 7: 509–520.
- Fortin MJ, Drapeau P. 1995. Delineation of ecological boundaries: comparison of approaches and significance tests. *Oikos* 72: 323–332.
- Gelman A, Carlin JB, Stern HS, Rubin DB. 2003. *Bayesian data analysis*. Boca Raton, FL, USA: Chapman & Hall.
- Hansen J, Nazarenko L, Ruedy R, Sato M, *et al.* 2005. Earth's energy imbalance: confirmation and implications. *Science* 308: 1431–1435.
- Higgins PAT, Mastrandrea MD, Schneider SH. 2002. Dynamics of climate and ecosystem coupling: abrupt changes and multiple equilibria. *Philosophical Transactions of the Royal Society of London, Series B* 357: 647–655.
- Hoffman WA, Schroeder W, Jackson RB. 2002. Positive feedbacks of fire, climate, and vegetation, and the conversion of tropical savanna. *Geophysical Research Letters* 29: 2052 (doi: 10.1029/2002/GL015424).
- IPCC. 2001. *Climate change 2001: the scientific basis. IPCC third assessment report: climate change 2001*. Cambridge, UK: Cambridge University Press.
- van de Koppel J, Rietkerk M, Weissing FJ. 1997. Catastrophic vegetation shifts and soil degradation in terrestrial grazing systems. *Trends in Ecology and Evolution* 12: 352–356.
- Krajick K. 2004. Climate change: all downhill from here? *Science* 303: 1600–1602.
- LaDeau SL, Clark JS. 2001. Rising CO₂ levels and the fecundity of forest trees. *Science* 292: 95–98.
- Mann MERS, Bradley RS, Hughes MK. 1998. Global-scale temperature patterns and climate forcing over the past six centuries. *Nature* 392: 779–787.
- Maslin M. 2004. Ecological versus climatic thresholds. *Science* 306: 2197–2198.
- Meehl GA, Washington WM, Collins WD, Arblaster JM, Hu A, Buja LE, Strand WG, Teng H. 2005. How much more global warming and sea level rise? *Science* 307: 1769–1772.
- O'Brien ST, Hubbell SP, Spiro P, Condit R, Foster RB. 1995. Diameter, height, crown, and age relationship in eight neotropical tree species. *Ecology* 76: 1926–1939.
- Pacala SW, Canham CD, Silander JA Jr, Kobe RK. 1994. Sapling growth as a function of resources in a north temperate forest. *Canadian Journal of Forest Research* 24: 2172–2183.

- Parmesan C, Yohe G. 2003. A globally coherent fingerprint of climate change impacts across natural systems. *Nature* **421**: 37–42.
- Platt WJ, Rathbun SL. 1993. Dynamics of an old-growth longleaf pine population. *Proceedings of the Tall Timbers Fire Ecology Conference* **18**: 275–297.
- Platt WJ, Strong DR. 1989. Gaps in forest ecology. *Ecology* **70**: 535.
- Platt WJ, Evans GW, Rathbun SL. 1988. The population dynamics of a long-lived conifer (*Pinus palustris*). *American Naturalist* **131**: 491–525.
- Runkle JR. 1981. Gap regeneration in some old-growth forests of the eastern United States. *Ecology* **62**: 1041–1051.
- Spiegelhalter DJ, Thomas A, Best NG, Gilks WR. 1995. *BUGS: Bayesian inference using Gibbs sampling*, Version 0.50. Cambridge, UK: MRC Biostatistics Unit.
- Swank WT, Crossley DA. 1988. Introduction and site description. In: Swank WT, Crossley DA, eds. *Forest hydrology and ecology at Coweeta*. New York, NY, USA: Springer-Verlag, 3–16.
- Valverde T, Silvertown J. 1997. Canopy closure rate and forest structure. *Ecology* **78**: 1555–1562.
- Ver Hoef JM. 1996. Parametric empirical Bayes methods for ecological applications. *Ecological Applications* **6**: 1047–1055.
- Walker B, Meyers JA. 2004. Thresholds in ecological and social-ecological systems: a developing database. *Ecology Society* **9**: 3. (<http://www.ecologyandsociety.org/vol9/iss2/art3>).
- Walther GR, Post E, Convey P, Menzel A, Parmesan C, Beebee TJC, Fromentin JM, Hoegh-Guldberg O, Bairlein F. 2002. Ecological responses to recent climate change. *Nature* **416**: 389–395.
- Wigley TML. 2005. The Climate change commitment. *Science* **307**: 1766–1769.

Author Query Form

Journal: New Phytologist

Article: `nph_1991(cow).fm`

Dear Author,

During the copy-editing of your paper, the following queries arose. Please respond to these by marking up your proofs with the necessary changes/additions. Please write your answers on the query sheet if there is insufficient space on the page proofs. Please write clearly and follow the conventions shown on the attached corrections sheet. If returning the proof by fax do not write too close to the paper's edge. Please remember that illegible mark-ups may delay publication.

Please read through the entire proof carefully, paying particular attention to the accuracy of equations, tables, illustrations (which may have been redrawn), other numerical matter and references (which have been corrected for style but not checked for accuracy, which remains the responsibility of the author).

Many thanks for your assistance.

| No. | Query | Remarks |
|-----|---|---------|
| 1 | Meehl et al. 2006 has been changed to Meehl et al. 2005 so that this citation matches the list | |
| 2 | Is the text OK now: the relationship may be piecewise linear, resulting in over-restricted ranges of tree diameters where the transitions between these linear regions are change-points | |
| 3 | define beta and sigma values? (e.g. the β parameters are regression coefficients. ...) | |
| 4 | Please resupply Figs. 4–7 in higher resolution version. For more information about supplying electronic artwork, please see the journal webpage or Blackwell's electronic artwork guidelines at http://www.blackwellpublishing.com/authors/digill.asp | |
| 5 | et al – please provide all author's names up to 20 | |

MARKED PROOF

Please correct and return this set

Please use the proof correction marks shown below for all alterations and corrections. If you wish to return your proof by fax you should ensure that all amendments are written clearly in dark ink and are made well within the page margins.

| <i>Instruction to printer</i> | <i>Textual mark</i> | <i>Marginal mark</i> |
|--|---|---|
| Leave unchanged | ... under matter to remain | Ⓟ |
| Insert in text the matter indicated in the margin | ∧ | New matter followed by ∧ or ∧ [Ⓢ] |
| Delete | / through single character, rule or underline or ┌───┐ through all characters to be deleted | Ⓞ or Ⓞ [Ⓢ] |
| Substitute character or substitute part of one or more word(s) | / through letter or ┌───┐ through characters | new character / or new characters / |
| Change to italics | — under matter to be changed | ↙ |
| Change to capitals | ≡ under matter to be changed | ≡ |
| Change to small capitals | ≡ under matter to be changed | ≡ |
| Change to bold type | ~ under matter to be changed | ~ |
| Change to bold italic | ≈ under matter to be changed | ≈ |
| Change to lower case | Encircle matter to be changed | ≡ |
| Change italic to upright type | (As above) | ⊕ |
| Change bold to non-bold type | (As above) | ⊖ |
| Insert 'superior' character | / through character or ∧ where required | Υ or Υ under character e.g. Υ or Υ |
| Insert 'inferior' character | (As above) | ∧ over character e.g. ∧ |
| Insert full stop | (As above) | ⊙ |
| Insert comma | (As above) | , |
| Insert single quotation marks | (As above) | ʹ or ʸ and/or ʹ or ʸ |
| Insert double quotation marks | (As above) | “ or ” and/or ” or ” |
| Insert hyphen | (As above) | ⊥ |
| Start new paragraph | ┌ | ┌ |
| No new paragraph | ┐ | ┐ |
| Transpose | ┌┐ | ┌┐ |
| Close up | linking ○ characters | Ⓞ |
| Insert or substitute space between characters or words | / through character or ∧ where required | Υ |
| Reduce space between characters or words | | ↑ |