Name: \_\_\_\_\_

This examination has 11 pages. Please check it as your first step.

Answers are to be written on the question paper, in the spaces provided.

Unless specifically asked to in a particular question, you do not need to <u>complete any detailed calculations</u>. Instead, answer as though you were setting up the computing task for your research assistant to complete.

If there is a possibility of ambiguity, be clear about 1- and 2-sided hypotheses, levels of confidence, degrees of freedom, whether 2 sample or 1 sample procedures, paired or unpaired, which table or formula from your textbook is relevant, etc.

Attempt all questions. The allocation of points will be as follows:

Q1 \_\_/10 Q2 \_\_/25 Q3 \_\_/20 (best 4 of the 5 portions a-e) Q4 \_\_/50 Q5 \_\_/25 (best 5 of the 6 portions a-f) Q6 \_\_/60 (best 6 of the 7 portions a-g)

total \_\_\_\_/180

Since the points add up to a total of 180, and since the examination is about 3 hours or 180 minutes, you can plan accordingly.

#### Q1 A new meaning for the abbreviation 'SE' ??? 10 POINTS

The following is part of a table in a recent paper from the Annals of Internal Medicine on a randomized placebo-controlled trial of low-dose aspirin in patients with chronic stable angina (paper courtesy of Leslie Brailsford)

"Baseline Characteristics of Participants with Chronic Stable Angina in the U.S. Physicians' Health Study

| Characteristic   | Aspirin Group<br>(n=119)                             | Placebo Group<br>(n=102)                             |
|--|--|--|
| Mean age, years<br>Mean systolic blood pressure, mm Hg<br>Mean diastolic blood pressure, mm Hg<br>Mean cholesterol level, mmol/L | $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$ | $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$ |

Plus-minus values are mean ± SE"

If you were checking this paper for typographical and other errors before it was published, what SE (Statistical Error !!!) would you have noticed?

### Q2 Judging the error in a measurement or average of measurements 15 POINTS

[If it helps, assume Gaussian variation for both parts of this question]

Say whether each assertion is true or false, and give a reason.

- a "If all you have is one measurement, you cannot estimate the likely size of the random error in it--you would have to take another measurement, and see how much it changes" 5 POINTS
- b "If all you have is one hundred measurements, you cannot estimate the likely size of the random error in their average--you would have to take another mean, and see how much it changes" 10 POINTS

#### Q3 Premature Death in Jazz Musicians 20 POINTS

"Comparison with national values showed that 70 (82%) of the musicians exceeded their life expectancy" (paragraph 7)

<u>Part 1</u>: Leave aside the possibility of a biased comparison. To keep it simple, consider a random sample (n=86) of persons (all of one specific race and sex) with a certain characteristic identified at birth in 1880, whose longevity is compared with the life expectancy (average lifetime) of their sex- and race-specific 1880 birth cohort. Also, assume that every one (including each of the 86) of the birth cohort is now dead and that you have the complete lifetable.

a What is the approximate shape of the frequency distribution of lifetimes in this 1880 birth cohort? 5 POINTS

b Choose an index (i.e. a measure) which summarizes the central tendency of lifetimes and formulate the null hypothesis in terms of this index. 5 POINTS

c Approximately (or precisely if you can say so) what percentage of the 1880 cohort lived past the index of central tendency for the cohort? Explain your answer. 5 POINTS

d For the index you chose, suggest a data-analysis which tests the hypothesis that persons with this certain characteristic of interest have shorter lifetimes than those in the 1880 birth cohort. 5 POINTS

e Suggest a 2nd index and give a corresponding test. 5 POINTS

### Q3 Premature Death in Jazz Musicians (continued)

<u>Part 2</u>: **OPTIONAL** (for students who wish to comment on validity of the comparison made by author) In <u>one or two sentences</u>, explain <u>one</u> bias in the author's comparison; and say whether it gives the jazz musicians an inbuilt longevity <u>advantage</u> or <u>dis</u>advantage?

[Hint: there are two biases: one explains why, on average, bishops live longer than priests (or full professors longer than assistant professors??); the other is because of the synthetic/artificial nature of lifetables]

### Q4 Paracetamol and Fever 50 POINTS

Entry was limited to children with temperatures between 38°C and 41°C.
 Given the mean of 38.9 °C and the SD of 0.9, what can you say about the shape of the frequency distribution over the 38°-41° interval?
 5 POINTS

| b | "We estimated a sample size requirement of 210 subjects completing  |
|---|---|
|   | the trial" (Sample size paragraph 5 of Methods)                     |
|   |   |
|   | Give the formula by which the authors estimated this (identify what |
| Í | numbers go with what parameters, but leave the details to your      |
|   | assistant [who has not taken a statistics course]) 5 POINTS         |

c "Student's t- test and Mann-Whitney (alias Wilcoxon) test..."
(Statistical testing -- paragraph 5 of Methods)
Why did the authors use the Mann-Whitney (alias Wilcoxon) test? In
light of the n's and the shape of the distribution of duration of
fever, was their concern about the use of the t test justified?
5 POINTS

# Q4 Paracetamol and Fever (continued)

d "The mean duration of fever..." [paragraph 4 of Results]

Explain in a sentence, in non-technical words, the phrase "the differences were statistically non-significant" 5 POINTS

e "The 95% CI for the differences between the paracetamol and placebo groups for duration of fever was -10.0 to +7.1 h"

Explain in non-technical words what this statement says. 5 POINTS

| f H | Iow | does | this | CI | add | to | what | is | shown | in | Fiqure | 1? | 5 | POINTS |
|-----|-----|------|------|----|-----|----|------|----|-------|----|--------|----|---|--------|
|-----|-----|------|------|----|-----|----|------|----|-------|----|--------|----|---|--------|

g How was the CI calculated? 5 POINTS

## Q4 Paracetamol and Fever (continued)

li

Before the study, the authors anticipated a SD of 2 days (48 hours)
 for the duration of fever. The SD of the duration of fever observed
 in the n=225 is not reported explicitly.

How could one reconstruct this SD from the results given [assume that the SD is the same in the two treatment groups]? 5 POINTS

"Children..were more likely to be rated.as having at least a 1category improvement in activity...." [2nd last paragraph of Results]

What tests could be used to compare the two groups? Do they all give the same answer? 5 POINTS

j "On the basis of ...completing the trial" [sample size considerations, first sentence of paragraph 5 of Methods]

"There were no significant differences between groups in mean duration of subsequent fever" [Abstract]

If these two statements were the ONLY information you were given about the trial, what could you conclude? 5 POINTS

# Q5 Melatonin and Delayed Sleep 25 POINTS

a What sample size formula or table would you have shown the authors if they had consulted you concerning sample sizes before doing their study? 5 POINTS

| b | What | is | it a | about  | the  | study | <sup>,</sup> desi | .gn | that  | make | es the | requi | red | sample |  |
|---|------|----|------|--------|------|-------|-------------------|-----|-------|------|--------|-------|-----|--------|--|
|   | size | so | much | n smal | ller | than  | that              | in  | Krame | er's | study  | 2 5   | PO  | INTS   |  |

| С | What do  | you  | consider | would   | be | а | clinically | significant | advance | in |
|---|----------|------|----------|---------|----|---|------------|-------------|---------|----|
|   | sleep on | iset | time?    | 5 POINT | ГS |   |            |             |         |    |

 d "In all 8 subjects sleep onset time was earlier during melatonin treatment than during placebo" [Abstract]
 List 3 possible tests of these data, putting them in order of increasing statistical power [do not carry out the tests, but give references] 5 POINTS

# Q5 Melatonin and Delayed Sleep (continued)

e Set up the calculation from which the p<0.01 for the 3.49 versus 2.12 [Table II, sleep onset time, melatonin versus placebo] was derived 5 POINTS

f Are there sufficient data in the table to allow you to verify the calculation? 5 POINTS

# Q6 Triazolam and Memory Impairment 60 POINTS

| a | "5 of the 6 | 5 , with a total of 12 episodes" [Abstract]   |
|---|-------------|---|
|   | Which is mo | ore statistically correct? Why? 10 POINTS   |
|   | (i)         | to base inferences from the observed rate of $5/6$ on the Binomial distribution with n=6?                                 |
|   | (ii)        | to base inferences from the observed rate of 40%<br>[12 episodes in 30 subject-drug nights]<br>on the Binomial with n=30? |

b "In the temazepam group there were no such episodes of memory impairment"

From these data, find a 95% confidence interval for the proportion <u>of persons</u> who will have episodes of memory impairment with this drug. 10 POINTS

| С        | "this rate for triazolam was statistically significant from those     |
|----------|---|
|          | for either the temazepam or placebo group (each p<0.05)" [3rd         |
|          | sentence, 2nd paragraph of Results daytime memory assessment]         |
|          |   |
| Ì        | What test would you perform here [limit yourself to triazolam versus] |
| Ì        | placebo; be clear about denominators, degrees of freedom, sample      |
| <u> </u> | sizes etc.]? 10 POINTS  |

d

g

### Q7 Triazolam and Memory Impairment (continued)

Convert the 12 observations in each row of the figure (top right, p829) into a separate 2x2 table for each subject. What statistical test would you perform on the data for each separate 2x2 table? Are such "n=1" tests legitimate?.

10 POINTS

e "a small sample size predisposes to type II error" [3rd paragraph of Discussion]

Use ordinary words to explain what type II error is, and why it is more likely with small n's. 10 POINTS

f Can a very small sample size predispose to type <u>I</u> error? [You may wish to use subjects 2 and 3 to make your point] 10 POINTS

What about Type I error with more moderate size samples? 10 POINTS

Q5 Limb-reduction defects and chorion villus sampling

SIR,--Dr Firth's report (March 30) on transverse limb-reduction defects after chorion villus sampling (CVS) at 56-66 days' gestation prompted us to examine our registry data. The possibility of an association between CVS and birth defects is a matter of such concern that a report of our preliminary findings is warranted. From 6604 cases of malformation reported in 1988-90 we selected the 118 with a transverse limb-reduction defect, this being the one in all of Firth's cases. The controls were the other 6486 malformed cases. 4 cases of limb-reduction and 15 controls were delivered after CVS (odds ratio 15.14, 95% confidence interval 4.18-49.65; p[Fisher's exact]=0.000305). (Letter to The Lancet Vol 337: May 4,1991)

a Write down the null hypothesis (in symbols, rather than in words)

b Write down an alternative hypothesis (again, in symbols). Say why you chose the one you did.

c Write down a table showing the reported data.

d List the other tables that Fisher's approach considers are even greater evidence for a positive association than the observed one.

- Q5 Limb-reduction defects and chorion villus sampling (continued)
  - e Write down the expression for, but do not calculate, the (conditional) probability of the observed table.

f What further calculation is needed to obtain the author's p-value (the author's alternative hypothesis is one sided)

g If the number of cases of limb-reduction delivered after CVS had been 6 rather than 4, would Fisher's Exact test have been indicated? Why/why not?