### Things They Don't Teach You in Graduate School

Ces choses qu'on ne vous enseigne pas aux études supérieures

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Department of Epidemiology, Biostatistics & Occupational Health Faculty of Medicine, McGill University

Sixth Canadian Statistics Student Conference Sixième congrès canadien des étudiants en statistique Université McGill | McGill University Montréal, Québec

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McGill University

#### Abstract

Much of what statisticians teach and use in practice is learnt 'on the job.' I recount here some of my early statistical experiences, and the lessons we might learn from them. They are aimed at those of you starting out in the profession today, and at the teachers who train you. I stress the importance of communication.

#### Key Words

### Fred Mosteller, Mentor '77-'80

communication; communication; communication.

### Steve Lagakos, Colleague '73-'80



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<sup>&</sup>lt;sup>1</sup>An expansion on some after-dinner remarks made at the Conference of Applied Statisticians of Ireland, held in Killarney, May 17-19, 2006. The article is dedicated to two former colleagues – and superb communicators – Fred Mosteller and Steve Lagakos, who are no longer with us.



# Lake | lac Ontario entre 1975 et 1977

http://www.biostat.mcgill.ca/hanley/SailingLakeOntario.mov

### Lagakos, interviewed by a biostatistics student as part of a Harvard course

http://www.biostat.mcgill.ca/hanley/Lagakos/leadershipInterviewTamarSofer.pdf

http://www.biostat.mcgill.ca/hanley/Lagakos/SteveLagakosInterview.WAV

# Mentor | Mentor

[Reprinted from RADIOLOGY, Vol. 143, No. 1, Pages 29-36, April, 1982.] Copyright 1982 by the Radiological Society of North America, Incorporated

James A. Hanley, Ph.D. Barbara J. McNeil, M.D., Ph.D.



The Meaning and Use of the Area under a Receiver Operating Characteristic (ROC) Curve<sup>1</sup>

101 101

# Mentor | Mentor HARVARDgazette

Campus & Community > Obituaries

### HSPH's Marvin Zelen dies at 87

### Was considered a 'tremendous force' in biostatistics

November 19, 2014 | Editor's Pick



Photo by Shaina Andelman

Harvard Professor Marvin Zelen was noted for developing the statistical methods and study designs that are used in clinical cancer trials, in which experimental drugs are tested for toxicity, effectiveness, and proper dosage.

#### HSPH Communications

Professor Marvin Zelen of the Department of Biostatistics at the Harvard T.H. Chan School of Public Health

# Topics in that piece | Les sujets dans cette partie

- Statistical Lineage, and Statistical History
- Green
- Jokes, and Other Teaching Tools
- 1st On-The-Job Lesson: Exact vs. Approx.

# <u>Communication</u>

Errors of Type III and Beyond

# Communication, Part II

Not in the Clinical Trials Textbooks

# <u>The Ten-Minute Consultation</u>

- Not the Usual Delta
- The Bigger Picture, and Other Media
- Sharing our statistical methods
- Tell Them What You Said

http://www.biostat.mcgill.ca/hanley/Reprints/
ThingsThevDontTeachYou-JHanley.pdf



### Plan

 <u>Selected</u> items from that piece  Sujets <u>choisis</u> de cette partie

STATISTICAL LEARNING

• L'APPRENTISSAGE DE LA STATISTIQUE

STATISTICAL PRACTICE

 LA PRATIQUE DE LA STATISTIQUE Classroom and Platform Performance Frederick Mosteller *The American Statistician* Vol. 34, No. 1 (Feb., 1980), pp. 11-17

 http://www.biostat.mcgill.ca/hanley/communicationCommunicationCommunication/ MostellerClassoomPlatform.pdf

https://www.umass.edu/wsp/resources/tales/mosteller.html

https://www.tandfonline.com/doi/abs/10.1080/00031305.1962.10479594

https://goo.gl/images/Ee4NCF

# Mentor | Mentor



# Maurice McGregor, MD

https://muhc.ca/newsroom/article/dr-maurice-mcgregor-faculté-médecine-l? université-président-l?unité-d?évaluation-technologie

http://www.cardiomuhc.ca/maurice-mcgregor

# How long did their hearts go on? A Titanic study

James A Hanley, Elizabeth Turner, Carine Bellera, Dana Teltsch

Several studies have examined post-traumatic stress in people who survive disasters but few have looked at longevity. The 1997 film *Titanic* followed one character, apparently fictional, but the longevity of the actual survivors, as a group, has not been studied. Did the survivors of the sinking of the *Titanic* have shortened life spans? Or did they outlive those for whom 14-15 April 1912 was a less personal night to remember?

### Subjects, methods, and results

We limited our study to passengers. We used data from biographies listed in Encyclopedia Titanica, a website that claims to have "among the most accurate passenger and crew lists ever compiled." Of the 500 passengers listed as survivors, 435 have been traced. We calculated the proportion alive at each anniversary of the sinking.

BMJ VOLUME 327 20-27 DECEMBER 2003 bmj.com

# Hazardous journeys

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University Elizabeth Turner graduate student



Year

Percentage still alive on each anniversary of sinking of *Titanic* among 435 survivors and Swedish and white American comparison groups matched for age and sex. Inset: analysis by sex and class of travel (n=No of passengers; age=median age in 1912)

# media

http://www.biostat.mcgill.ca/hanley/bios602/ b-d-II-ch-1-2-3/InterviewGlobalTV.mov

http://www.biostat.mcgill.ca/hanley/bios602/ b-d-II-ch-1-2-3/radioCanadaInternational.mp3

# Hazardous journeys

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Year

Percentage still alive on each anniversary of sinking of *Titanic* among 435 survivors and Swedish and white American comparison groups matched for age and sex. Inset: analysis by sex and class of travel (n=No of passengers; age=median age in 1912)

the Freedom Tower vesterday, but the "world's highest" building, to replace the World Trade Centre buildings, is actually 12 metres shorter than Toronto's CN Tower. Page A25



#### INDEX

| Annie's Mailbox F7    | Legals/AuctionsF5  |
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| CareersB7             | Obituaries B21-B23 |
| Classified FI         | Opinion A31        |
| Comics . Life 10-12   | Pop Culture D1     |
| Crosswords C7, E7, F2 | SportsCl           |
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| Homefront El          | Wonderword F4      |
| Horoscope F4          | World A22          |



SATURDAY, DECEMBER 20, 2003 MONTREAL

Carl Napoleon, manager of the

Rogers cell-phone shop across

Please see SNOW, Page A4

Titanic

Trauma didn't affect

lifespan, study finds

AARON DERFEL

GAZETTE HEALTH REPORTER Yes, their hearts did go on.

McGill University researchers

have discovered that most survivors of the sinking of the Ti-

tanic ended up living long, full

In fact, most slightly outlived

average Americans of their time

who were never involved in a dis-

The findings - published in

yesterday's British Medical Journal - contradict assump-

tions that post-traumatic stress

disorder might have cut short

Please see TITANIC, Page A4

lives after the 1912 tragedy.

aster

their lives.

the street

QUEBEC'S OLDEST DAILY

SINCE 1778 FIRST EDITION

RICHARD ARLESS JR. THE GAZETTE On Ste. Catherine St. near Peel St. yesterday: The one million people who pass through the city's

51. 50 hit they ways o what's l it's beer nast cor Howe know w or, mor days, a bles a l nibblir he's g one n through are slit double officer would the hul

Plca

10 tir

more

than

centre are slipping, sliding and almost double-lutzing their way to the office or Christmas shopping. Cintec's latest controversy

survivors Waste-management firm blames probes led long lives of Salvadoran landfill on bare-knuckles politics

For breaking

news, updated Gazette stories

and more, 24/7:

canada.con

DON MacDONALD THE GAZETTE

Money laundering, drug trafficking, municipal corruption: the allegations and innuendo hanging over Montreal waste-management company Cintec Group could hardly be more serious. Cintec operates the largest landfill in the tiny Central American country of El Salvador. For a year, the company and the landfill project have been bombarded by dozens of damaging headlines in Salvadoran newspapers and been made the subject of no fewer than three offi-

Paper tried to dig up dirt, Page A3

OHOTE Terrible is the temptation to be good. Bertolt Brecht WEATHER Sunny breaks High -7º Low -13º Page C7 \$2 | Beyond metropolitan area \$2.30 Offer ands December 31, 2003. Subject to a 24 month service agreement. Details in store

cial investigations. Please see GARBAGE, Page A2 That's up by 15 per-

trians continue to feel that there are unigrants coming. 4 per cent, up from n a June survey),"

the recent election.

The Conservative platform promised to bring "good people into Ontario while keeping bad people out." The document also slammed the federal government, which has jurisdiction

saying about the right number of immigrants were entering the country

and the territories were most inclined to see immigration levels as being about right (46 per cent, down from 50 per cent). That

ly than men - 42 versus 34 per cent, respectively to feel that "too many" immigrants come to Residents of British Columbia Canada, particularly those over 35 years of age.

Also consistent with previous findings is that Canadians with a higher level of education are less

amount fell to 38 per cent from 47 per cent.

The national poll of 1.675 Canadians was conducted Sept. 2-7 by Pollara and is considered accurate within 2.4 percentage points, 19 times out of 20. OTTAWA CITIZEN

# nayor speed sval

tions make it hardters.

r to do our job on ave been cleared." tients cancelled aphis week at a radiolthe Seaforth buildes Neiges Rd. w older folk looked low, saw the snow they didn't want to Mary Gibson, a re-Seaforth Radiology

ndoor parking off ... she said, but the low priority for borews. it worse," Gibson

really bad, it's hard ucople deal with it sigh and wait for it

carrol(@ le.canwest.com



vices unhlad

COURTESY OF 20TH CENTURY-FOX A scene from the 1998 movie Titanic. Taking a cue from the blockbuster, researchers studied the longevity of first-, second- and thirdclass passengers, and their findings fly in the face of conventional wisdom that the privileged lead longer lives.

### JUDICU rupted

# **Titanic** | 'This was a survival of the fittest'

in-more snow wallop disrupted adaptedces and some regular n Montreal Island sential services for ssengers were canweek because of the id road conditions. 'aradis, a Montreal a spokesperson wities were getting

edical appointments " she said - meaning transit services for leisure trins heltered workshops tellectually handie also cancelled she access roads had not 1 and the people are d on their feet." panies, which nortle 60 per cent of

isit, couldn't keep up ulverse driving conincreased customer radis said. as routes also experiand disruptions. ad 211 buses on Lake-

) Beaconsfield were of St. Charles Blvd.. 1. "There was no salt vas a skating rink." ighter side, the subwas husier than usu. ne of year, she said. t snow in the métro e fewer delays "

#### CONTINUED FROM A1

Taking a cue from Titanic, the 1997 movie blockbuster starring Leonardo DiCanrio and Kate Winslet, researchers also examined the longevity of first-second- and third-class passengers. Again, the findings fly in the face of conventional wisdom that the privileged lead longer lives.

Whether a Titanic passenger sailed steerage - like Jack Dawson, the fictional film character portraved by DiCaprio - or sipped champagne - like Winslet's young socialite, Rose De Witt Bukater - survivors in all classes ended up living just as long.

James Hanley a statistician in McGill's department of epidemiology and biostatistics, said the lives of Titanic survivors have been investigated so thoroughly. they are ideal candidates for a longevity study.

"Did the experience they have would it mean they're so hardened and so lucky and so thankful that they're going to live forever like the song says?" Hanley asked He was referring to the film's treacly power ballad. My Heart Will Go On, performed by Que-

bec's chest-thumping chanteuse. Céline Dion "Or." Hanley continued, "were they so traumatized and the men so guilt-ridden" they would die

prematurely?

To answer those questions, he and three graduate students pored through a trove of biographical data in the Encyclopedia Titanica, a Web site claiming to have "among the most accurate passenger and crew lists ever compiled" of the voyage.

The researchers compared the longevity of 435 of the 500 survivors with control groups in the United States and Sweden

The study showed that, on average, a Titanic survivor lived 1.7 years longer than someone in the general population in the United States at the time of the sinking and half a year longer than a member of a similar group in Sweden.

More than half of the survivors lived well into their 70s roughly equal to the longevity of the comparison groups.

Five people lived past 100, and the three remaining survivors are now in their 90s. They're all female - to be expected, given that women have a higher life expectancy than men. Two sailed in third class, one in second.

Hanley who sailed on the Queen Elizabeth II from New York to London in 1999, said the results suggest the tragedy was consistent with the Darwinian theory of survival of the fittest. "These are lucky people who

### TITANIC SURVIVORS DIE AT NORMAL RATE

Percentage still alive on each anniversary of the sinking of the Titanic among 435 survivors, and Swedish and white American comparison groups matched for age and sex



THE GAZETTE

were going to live a long time. who were going to value their lives and were going to be doubly careful," he explained.

"Some people have said this was a survival of the fittest and that, of course, the survivors were going to do well."

The study also turned on its head the notion that the affluent - who can afford the best health care and who eat better than the underprivileged - live longer:

"We immediately thought the survivors of first and second class would do very well because they are so privileged." Hanley said. "The upshot is that this first-class team wasn't very first class."

The study was published in the journal's end-of-the year edition, reserved for offheat research papers.

> aderfel@ thegazette.canwest.com

# re doesn't seem to be any pattern, any plan,' cop says

her treated burkers de de nov banks work passable to all but - one had touched it

nettern and abay You Havalla alone one block and its time setto the contract and it. I the me-

In reaction to the city's appar ent letharey, local merchants. have started in me their own ner sonnel to at least clear the patch.

route an ambulance down Ste. Catherine St."

Emergency volucles might have had a difficult time of 0 this

bination of heavy snowfall. freezing rain and sudden freezes. since Monday

But for people like Parker, who

# Les survivants du *Titanic* s'en sont bien sortis

#### MATHIEU PERREAULT

A 14

Ouand il a vu le film Titanic, avec Leonardo di Caprio et Kate Winslet, James Hanley s'est demandé de quelle manière la catastrophe avait marqué les survivants du naufrage. Son réflexe est bien normal : M. Hanley est professeur d'épidémiologie à l'Université McGilL

Quelques années plus tard, il a trouvé le moven d'élucider la question. Il a trouvé, sur Internet une liste de biographies de la presque étudiants : en raison du traumatisme du naufrage, les survivants du Titanic ont-ils vécu moins longtemps que la population moyenne 2

La réponse a surpris M. Hanley : la catastrophe ne semble pas avoir affecté la longévité des passagers. « On pourrait s'attendre à ce que la mort de membres de la famille. l'attente dans l'eau glacée, ou le sentiment de culpabilité à l'idée d'avoir eu la chance d'échapper au sort horrible des novés, affecte la vie, et donc la longévité, des survivants. Mais nos calculs montrent que non. Ca amène de l'eau au moulin des gens qui disent que le concept de stress post-traumatique lone terme a

#### Recherches plus légères...

numéro du British Medical Journal, une prestigieuse revue médicale qui consacre ses numéros de Noël à méro de cette année comporte notamment une étude des panneaux que notre article est pertinent, »

routiers indiquant les zones où vivent de nombreuses personnes ânées.

LAPRESSE MERCREDI 24 DÉCEMBRE

L'analyse des données du site Encyclopedia Titanica n'est pas terminéc. « Je veux vérifier si la longévité est la même pour les survivants ayant perdu des membres de leur famille, et si le survivant était enfant ou adulte en 1912 », dit M. Hanley, qui a un grand intérêt pour l'océan et les paquebots depuis son enfance sur une ile irlandaise. Une analyse de la classe sociale des survivants laisse déjà entrevoir que totalité des passagers du Titanic. Il plus le survivant est riche, plus il a ensuite posé une question à ses est affecté par le traumatisme : les survivants de première classe ont la même longévité que ceux de troisième, alors qu'on pourrait s'attendre à ce que les riches de cette époque vivent plus longtemps que les pauvres.

L'étude de l'impact de certains événements sur la longévité est un champ de l'épidémiologie qui gagne en importance. « Il y a notamment un épidémiologiste torontois. Don Redelmeier, qui a étudié l'impact de gagner un Oscar et celui d'être le président d'une classe de médecine, dit M. Hanley, Les gagnants des Oscars vivent quatre ans plus vieux que ceux qui n'avaient eu qu'une nomination : dans le deuxième cas, la charge de présin'entraîne pas de conséquences à dent a un effet négatif, elle enlève deux ans à l'espérance de vie. »

Ce domaine pointu n'est pas exempt de controverses, « Redel-L'épidémiologiste et ses étudiants meier a dit à Discovery Channel publient leur étude dans le dernier que mon étude n'est pas valable parce que mon analyse exclut 17 % des survivants, pour lesquels on n'a pas de données, indique M. des recherches plus légères. Le nu- Hanley. Je suis d'accord qu'il faut affiner les analyses, mais je pense

STATISTICAL LEARNING | L'APPRENTISSAGE DE LA STATISTIQUE

# STATISTICAL LEARNING

# L'APPRENTISSAGE DE LA STATISTIQUE

- Minimalist
- Real-life props
- Simulations/Animations
- Unity/Logic
- Curiosity

- Minimaliste
- Accessoires dans la vraie vie
- Simulations/Animations
- Unité/Logique
- Curiosité

# Minimalist... examples

# Minimaliste... exemples

• 
$$E\left[\frac{\sum(y-\bar{y})^2}{n}\right] = \frac{n-1}{n}\sigma^2$$

n = 2; y ∈ (0,1) or (1,2,3)
http://www.biostat.mcgill.ca/
hanley/c607/ch01/mm\_ch\_01.pdf page 4

• Structure of  $\hat{\beta}$  &  $Var[\hat{\beta}]$ when fitting  $E[Y|X] = \beta X$ using various criteria

Fit Model with  $\underline{1}$  para to dataset with  $n = \underline{2}$ 

```
y x
------
2 1
8 2
```

http://www.biostat.mcgill.ca/
/hanley/2DatapointsAndaModel/

# • GEE: heights(y) of *n* = 3 children in 2 families

http:

```
//www.biostat.mcgill.ca/hanley/
Reprints/aje_gee_orientation.pdf
```

• 
$$E\left[\frac{\sum(y-\bar{y})^2}{n}\right] = \frac{n-1}{n}\sigma^2$$

```
n = 2; y ∈ (0,1) où (1,2,3)
http://www.biostat.mcgill.ca/hanley/
c607/ch01/mm_ch_01.pdf page 4
```

• Structure de  $\hat{\beta} \& Var[\hat{\beta}]$ lors de l'ajustement de  $E[Y|X] = \beta X$ en utilisant divers critères

Ajuster Modèle avec  $\underline{1}$  para au jeu de données avec n =  $\underline{2}$ 

| У | Х |
|---|---|
|   |   |
| 2 | 1 |
| 8 | 2 |

http://www.biostat.mcgill.ca/
/hanley/2DatapointsAndaModel/

# • GEE: Taille(y) de *n* = 3 enfants de 2 familles

http://www.biostat.mcgill.ca/hanley/
Reprints/aje\_gee\_orientation.pdf

### Real-life props / Visualizations

# Elevators (L<sub>1</sub> vs. L<sub>2</sub> norm, CLT)

http://www.medicine.mcgill.ca/
epidemiology/hanley/elevator.html

### Travel times/distances (CLT, Gamma ↔ Poisson)

http://www.biostat.mcgill.ca/hanley/ bios601/Mean-Quantile/clt\_in\_action\_ 1.gif

http://www.biostat.mcgill.ca/hanley/ bios601/Mean-Quantile/EnoughTires. html

### Ages/recency of books MPG ↔ litres/100Km °F ↔ °C ( Change of Scale, Jacobians )

http://www.biostat.mcgill.ca/hanley/
Reprints/jh\_dt\_tas\_2006.pdf

### Accessoires dans la vraie vie / Visualisations

# Ascenseurs (norme *L*<sub>1</sub> *vs*. *L*<sub>2</sub>, TCL )

http://www.medicine.mcgill.ca/
epidemiology/hanley/elevator.html

### Temps de déplacements/distances (TCL, Gamma ↔ Poisson)

http://www.biostat.mcgill.ca/hanley/ bios601/Mean-Quantile/clt\_in\_action\_ 1.gif

http://www.biostat.mcgill.ca/hanley/ bios601/Mean-Quantile/EnoughTires. html

### Âges/récence des livres MPG ↔ litres/100Km °F ↔ °C ( Changement d'échelle, Jacobiens )

http://www.biostat.mcgill.ca/hanley/
Reprints/jh\_dt\_tas\_2006.pdf

# Real-life props / Visualizations

### Words in Text (Length-bias)

http://www.biostat.mcgill.ca/hanley/ bios601/Surveys/newsweek.pdf

### % and depth of ocean (CLT, CDF<sup>-1</sup> sampling)

http://www.biostat.mcgill.ca/hanley/ Reprints/HowDeepIsTheOcean.pdf http://www.biostat.mcgill.ca/hanley/ bios601/Surveys/Oceanography/

### Lotteries

### (E, V, multiplicity, .... )

http://www.biostat.mcgill.ca/hanley/
Reprints/jumping\_to\_coincidences.pdf

### • N(·,·): s<sup>2</sup> ~ Gamma (Fisher)

http://www.biostat.mcgill.ca/hanley/
Student/

HanleyEtAlStudent-FishersDerivation.

### Accessoires dans la vraie vie / Visualisations

 Mots en Texte (Biais de longueur)

> http://www.biostat.mcgill.ca/hanley/ bios601/Surveys/newsweek.pdf

### % et profondeur de l'océan (TCL, échantillonnage FR<sup>-1</sup>)

http://www.biostat.mcgill.ca/hanley/ Reprints/HowDeepIsTheOcean.pdf http://www.biostat.mcgill.ca/hanley/ bios601/Surveys/Oceanography/

# Loteries (E, V, multiplicité, ....)

http://www.biostat.mcgill.ca/hanley/
Reprints/jumping\_to\_coincidences.pdf

# • $N(\cdot,\cdot)$ : $s^2 \sim$ Gamma (Fisher)

http://www.biostat.mcgill.ca/hanley/ Student/

HanleyEtAlStudent-FishersDerivation.



http://www.biostat.mcgill.ca/hanley/Reprints/Accromath-2015-1-4.pdf

http://www.biostat.mcgill.ca/hanley/bios601/Mean-Quantile/forAccromathBackTranslate.pdf

# Simulations/Animations

### Cell Occupancy

http://www.biostat.mcgill.ca/hanley/ bios601/Intensity-Rate/ Randomly selected visits to 1000 cells

### Epidemics, Cards, Gambling, Lotteries http: //www.biostat.mcgill.ca/hanley/c323/

### Chevalier de Méré

http://www.biostat.mcgill.ca/hanley/ bios601/Proportion/ChevalierDeMere.R. txt

### Bridge of Life

http://www.biostat.mcgill.ca/hanley/
BridgeOfLife/

### Cancer Screening

http://www.biostat.mcgill.ca/hanley/
screening/ bottom of page

# Simulations/Animations

- Occupation des cellules
   http://www.biostat.mcgill.ca/
   hanley/bios601/Intensity-Rate/ Visites
   choisies au hasard à 1000 cellules
- Épidemies, cartes, paris, loteries http://www.biostat.mcgill.ca/ hanley/c323/

### Chevalier de Méré

http://www.biostat.mcgill.ca/
hanley/bios601/Proportion/
ChevalierDeMere.R.txt

### • Le pont de la vie

http://www.biostat.mcgill.ca/
hanley/BridgeOfLife/

# Dépistage du cancer

http://www.biostat.mcgill.ca/ hanley/screening/ au bas de la page

# Unity/Logic

• 
$$\widehat{Var[\hat{\mu}]} = \frac{s^2}{n}$$
;  $\widehat{Var[p]} = \frac{p(1-p)}{n}$ 

 Sample size power considerations

http:

//www.biostat.mcgill.ca/hanley/
Reprints/UniversalSampleSize.pdf

Mother of all regressions

 $g(E[y]) \sim 1$ 

- Survival analysis ≠ special topic (esp. if one uses ML to fit models)
- Info. (1) rather than  $Var = I^{-1}$



# Unité/Logique

• 
$$\widehat{Var[\hat{\mu}]} = \frac{s^2}{n}$$
;  $\widehat{Var[p]} = \frac{p(1-p)}{n}$ 

• Considérations pour la taille d'échantillon/puissance http:

//www.biostat.mcgill.ca/hanley/
Reprints/UniversalSampleSize.pdf

• Mère de toutes les régressions

 $g(E[y]) \sim 1$ 

- Analyse de survie ≠ sujet spécial (spéc. si on utilise MV pour ajuster modèles)
- Info. (1) au lieu de  $Var = I^{-1}$



### Curiosity

Measurement Errors:

$$F=32+\frac{9}{5}C$$

http://www.biostat.mcgill.ca/ hanley/bios601/Surveys/ ErrorsInXAnimation.R.txt

### • 1.08 × Woman (Galton)

http://www.biostat.mcgill.ca/ hanley/galton/

### History

### http:

//www.biostat.mcgill.ca/hanley/ http://www.biostat.mcgill.ca/ /hanley/anniversaries/

# Curiosité

Erreurs de mesure:

$$F=32+\frac{9}{5}C$$

http://www.biostat.mcgill.ca/ hanley/bios601/Surveys/ ErrorsInXAnimation.R.txt

### • 1.08 × Femme (Galton)

http://www.biostat.mcgill.ca/ hanley/galton/

### Histoire

http:

//www.biostat.mcgill.ca/hanley/ http://www.biostat.mcgill.ca/ /hanley/anniversaries/



### TABLE I.

NUMBER OF ADULT CHILDREN OF VARIOUS STATURES BORN OF 205 MID-PARENTS OF VARIOUS STATURES. (All Female heights have been multiplied by 1.08).

| Heights of<br>the Mid- |           | Heights of the Adult Children. |      |      |      |      |      |      |      |      |      |      | Total Number of |      | Madiana  |                    |                  |      |
|------------------------|-----------|--------------------------------|------|------|------|------|------|------|------|------|------|------|-----------------|------|----------|--------------------|------------------|------|
| inches                 | 111<br>1. | Below                          | 62.2 | 63.2 | 64.2 | 65-2 | 66-2 | 67.2 | 68.2 | 69.2 | 70.2 | 71.2 | 72.2            | 73.2 | Above    | Adult<br>Children. | Mid-<br>parents. | 1999 |
| Above                  |           |                                |      |      |      |      |      |      |      |      |      |      | 1               | 3    | 3. j. j. | 4                  | 5                |      |
| 72.5                   | 336       | · · · ·                        | 1    |      |      |      |      |      | 1    | 2    | 1    | 2    | 7               | 2    | 4        | 19 .               | 6                | 72.2 |
| 71.5                   | 213       | Sec. Oak                       |      |      |      | 1    | 3    | 4    | 3    | 5    | 10   | 4    | 9               | 2    | 2        | 43                 | 11               | 69.9 |
| 70.5                   |           | 1                              |      | 1    |      | 1    | 1    | 3    | 12   | 18   | 14   | 7    | 4               | 3    | 3        | 68                 | 22               | 69.5 |
| 69.2                   |           |                                |      | 1    | 16   | 4    | 17   | 27   | 20   | 33   | 25   | 20   | 11              | 4    | 5        | 183                | 41               | 68.9 |
| 68.5                   | 18 A      | 1                              |      | 7    | 11   | 16   | 25   | 31   | 34   | 48   | 21   | 18   | 4               | 3    | ••       | 219                | 49               | 68.2 |
| 67.5                   |           | ••                             | 3    | 5    | 14   | 15   | 36   | 38   | 28   | 38   | 19   | 11   | 4               |      | ••       | 211                | 33               | 67.6 |
| 66.2                   |           | ••                             | 3    | 3    | 5    | 2    | 17   | 17   | 14   | 13   | 4    |      | ••              |      | ••       | 78                 | 20               | 67.2 |
| 65.2                   |           | 1                              | 1    | 9    | 5    | 7    | 11   | 11   | 7    | 7    | 5    | 2    | 1               |      |          | 66                 | 12               | 66.7 |
| 64.5                   |           | 1.0                            | 1    | 4    | 4    | 1    | 5    | 5    |      | 2    |      |      |                 |      |          | 23                 | 5                | 65.8 |
| Below                  | ••        | 1                              |      | 2    | 4    | 1    | 2    | 2    | 1    | 1    | ••   | ••   | ••              |      | S •• 10  | 14                 | 1                |      |
| Totals                 |           | 5                              | 7    | 32   | 59   | 48   | 117  | 138  | 120  | 167  | 99   | 64   | 41              | 17   | 14       | 928                | 205              | ••   |
| Medians                |           |                                |      | 66.3 | 67.8 | 67.9 | 67.7 | 67.9 | 68.3 | 68.5 | 69.0 | 69·0 | 70.0            |      | ••       |                    |                  |      |

NOTE.—In calculating the Medians, the entries have been taken as referring to the middle of the squares in which they stand. The reason why the headings run 62.2, 63.2, &c., instead of 62.5, 63.5, &c., is that the observations are unequally distributed between 62 and 63, 63 and 64, &c., there being a strong bias in favour of integral inches. After careful consideration, I concluded that the headings, as adopted, best satisfied the conditions. This inequality was not apparent in the case of the Mid-parents.

|     |         | (ad       | FAMILY HEIGHTS.             | from RFF                      |
|-----|---------|-----------|-----------------------------|-------------------------------|
|     | Father  | Mether    | Some in order of height     | Daughters in order of height. |
| 1   | 18.5    | 7.0       | 13-2                        | 9.2, 9.0, 9.0                 |
| 2   | 15.5    | 6.5       | 13.5, 12.5                  | 5.5 5.5                       |
| 3   | 15.0    | about 40  | 11-0                        | 8.0                           |
| 4   | 15.0    | 4.0       | 10.5, 8.5                   | 7.0, 4.5, 3.0                 |
| 5   | 15.0    | -1.5      | 12.0, 9.0, 8.0              | 6.5, 2.5, 2.5                 |
| 6   | 14.0    | 8.0       |                             | 0.5                           |
| 7   | 14.0    | 8.0       | 16.5, 14.0, 13.0, 13.0      | 10.5. 4.0                     |
| 8   | 14.0    | 6.5       | 10 00 10 10 10              | 10.5. 8.0. 6.0                |
| 9   | 14.5    | 6.0       |                             | 6.0                           |
| 0   | 14-0    | 5.5       |                             | 5-5                           |
| 1   | 14.0    | 2.0       | 14.0, 10.0                  | 8.0, 7.0, 7.0, 6.0, 3.5, 3.   |
| 12  | 14.0    | 1:0       |                             | 5-0                           |
| 1   |         |           |                             |                               |
| 13  | 13-0    | 7.0       | 11.0                        | 2.0 GALTON P                  |
| 14  | 13:0    | 7.0       | 8.0, 7.0                    | and market                    |
| 15  | 13.0    | 6.5       | 11.0, 10.5                  | 6.7                           |
| 16  | 13.0    | about 5.0 | 12.0, 10.5, 10.2, 10.2, 9.2 | 8.7, 6.5, 4.5, 3.5            |
| 17  | 13.0    | 4.5       | 14.0, 13.0, 11.5, 2.5       | 6.5, 2.3                      |
| 18  | 13-0    | 4.0       |                             | 6.0, 4.5, 4.0                 |
| 19  | 13-2    | 3.0       |                             | 2.7                           |
| 20  | 12.7    | 9.0       | 13.2, 13.0, 12.7            | 10.0, 9.0, 8.5, 8.0, 6.0      |
| 21  | 12.0    | 8:0       | 13.0                        | 2.5, 8.0                      |
| 22  | 12.0    | alt. 7.0  | 13.0, 11.0                  | 7.0                           |
| 25  | 12.0    | 5.0       | 14.2, 10.5, 9.5             | 6.0, 5.5, 5.0, 5.0 .,         |
| 24  | 12.0    |           |                             |                               |
|     |         |           |                             |                               |
| THE | and all | about the |                             |                               |

| 1 | Taller        | Meller   | Soo in order of height               | Daughters in outer of purpht      |
|---|---------------|----------|--------------------------------------|-----------------------------------|
| 5 | 10.5          | 3.0      | 12.5. 0.0. 710                       | 16.14                             |
|   | 10.0          | 3.5      | 11.0, 7.5                            | 2.6 1.5                           |
|   | 10.0          | 3.0      | 8.0, 7.0                             | 3.2 2.0                           |
|   | 10:0          | 3.0      | 10.0, 6.5                            | 2.0. 1.0                          |
|   | 10.5          | 2.0      | 12.0, 100, 9.5, 9.5, 8.0             | 5.0. 4.0. 3.0                     |
|   | 10.3          | 2.7      | 10.7, 97, 92, 52                     | 4.0. 3.5. 3.2                     |
|   | 10.5          | 2.0      | ast. 12.0, alt. 12.0                 | 0.0                               |
|   | 10.0          | 1.0      | 11:2, 7:0                            | Tall                              |
|   | 10.0          | 0.0      | 7.0, 4.5                             | 5.0, 3.0                          |
|   | abt: 10 0     | 0.0      |                                      | 5.0, alt. 5.0                     |
|   | 10.0          | -1.5     | 11:5, 4:5                            | 3.0, deformed                     |
|   | 10.0          | -2.0     | 12.0, 6.0                            | 6.0, 5.0, 3.0                     |
|   |               |          |                                      |                                   |
|   | 9.0           | 8.5      | 15.0, 11.0, 10.0                     | 6.0, 6.0, 5.5, 5.0, 5.0, 4.0, 4.0 |
|   | 9.0           | 7.0      |                                      | 4.0                               |
|   | 9.0           | 6.0      | 13.0, 12.0, 11.7, 11.5               | 5.5, 5.0, 2.7, 2.5                |
|   | 9.0           | 6.0      | 11.2, 11.0, 10.0                     |                                   |
|   | 9-0           | 6.7      | 15.0, 14.0, 12.0, 8.5                |                                   |
|   | 9.0           | 6.0      | 10:0, 8.5, 8.0                       | 5.0, 3.0, 2.5                     |
|   | 9.0           | 6.5      | abt. 12.0, 11.0, alt. 105, abt. 105, | abt. 1-0                          |
|   | 9.5           | 6.5      | 10'5, 7.5                            | 4.5. 4.0                          |
|   | 9.0           | 6.5      | 11:0                                 | 8.5. 7.5. 6.0. 3.0. 3.0           |
|   | 9.5           | 6.0      | 11.0, 11.0, 10.5, 10.5               | 6.5. 5.5. 4.5                     |
|   | 9.0           | 6.0      | 13.0, 12.0, 9.0, 9.0                 | 6.5, 5.5, 5.5, 5.0, 4.0           |
|   | 9.0           | 5.0      | 10.0, 8.5, 7.0                       | 5-0, 4.0, 3.5 1.0                 |
|   | 9.5           | 4.5      | 9.7. 8.0. 0.0                        | 5.2 4.5 3.7 0.0                   |
|   | 9.2           | ast. 4.0 | 11.2. 6.5                            | 50, 35                            |
|   | 9.0           | 3.5      |                                      | 5.5                               |
|   | 9.0           | 3.0      | 9.0                                  | 9.5 3.5                           |
| a | At.g.o        | 3.0      | 12.0                                 |                                   |
| 6 | K. 9.0        | alt. 3.0 | 13.0 10.0 10.0 alt 1.0               |                                   |
|   |               |          | 122 122 142 T                        | 1000 000 210                      |
|   | Second Second | -        |                                      |                                   |

| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | Na  | Father | Mether | Sens in ord |
|--|--|-----|--------|--------|-------------|
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | 73  | 6.0    | 7.0    | 12.0. 5.0   |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $\begin{array}{cccccccccccccccccccccccccccccccccccc$   | 74  | 6.0    | 6.0    | 6.0, 5.0    |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$   | $\begin{array}{cccccccccccccccccccccccccccccccccccc$   | 75  | 6.0    | 6.0    | 12.0. 8.0.  |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $\begin{array}{cccccccccccccccccccccccccccccccccccc$   | 76  | 6.5    | 5-0    | 87. 8.5.4   |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$   | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | 77  | 6.0    | 5.5    | 12.0, 11.0. |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $\begin{array}{cccccccccccccccccccccccccccccccccccc$   | 178 | 6.0    | 3.0    | 10.0        |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | 79  | 6.0    | 3.5    |             |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$   | $\begin{array}{cccccccccccccccccccccccccccccccccccc$   | 80  | 6.5    | 3.0    | 7.2. 7.0.   |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | 81  | 6.5    | 2.5    | 10.0, 8.0   |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | 82  | 0.0    | 1.5    | 10.0        |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | 83  | 6.0    | 0.0    | 8.0. 7.0.   |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $\begin{array}{cccccccccccccccccccccccccccccccccccc$   | 84  | 6.0    | 0.0    | 5.0         |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$   | 10         100         100           10         40         70         40         10           10         40         70         40         10         10           10         40         10         10         10         10         10           10         40         10 <td>85</td> <td>6-0</td> <td>-1.0</td> <td>8.0. 4.0 0</td>   | 85  | 6-0    | -1.0   | 8.0. 4.0 0  |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  |     |        |        | 2 2 1 2 2   |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | 86  | 5.0    | 7.0    | 6.5 b.0     |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $\begin{array}{cccccccccccccccccccccccccccccccccccc$   | 87  | 5.0    | 7.0    |             |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | 88  | 5.0    | 6.0    | 2.0         |
| 10         10< | 1         4.4         4.5  | 80  | 5.0    | 6.0    | 20          |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | 20  | 5.0    | 50     | 00 00       |
| 2         4.4         5.8         4.4         25         7.4           3         5.4         4.4         25         7.6         7.6           3         5.4         4.4         25         7.6         7.6           5         5.4         4.4         25         7.6         7.6           5         5.6         5.6         7.6  | 1         3         3         3         3         4         2         3         4         4         75         75         3         3         4         4         75         75         3         3         4         4         75         75         75         3         3         4         76         75         76         3         3         4         76         75         76         3         3         4         76         3         3         4         76         3         3         4         3         4         3         6         3         4         3         4         3         4         3         4         3         4         3         4   | 21  | 5.0    | 60     | 4           |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$   | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | 1º  | 100    |        | 1. la       |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$   | 3         4.4         76         76.4           5         5         5         6         7.6           7         5         5         6         1.6         1.6           7         5         5         6         1.6         1.6         1.6           7         5         5         6         1.6 <td>-</td> <td>5.0</td> <td>3.0</td> <td>22, 20</td>   | -   | 5.0    | 3.0    | 22, 20      |
| 7 54 50 149<br>7 54 30 56, 50<br>1 55 30 140, 140, 140,<br>7 55 00 50, 70,<br>7 4.0 4.0 110, 53<br>7 4.0 4.0 10, 53<br>4.40 4.0 4.5<br>4.40 0.0 59   | 7 54 56 her<br>7 54 56 6e, 6e,<br>4 55 30 her her<br>5 55 68 9e, 2e,<br>7 44 4e her her<br>1 44 4e her<br>1 44 5<br>44 5<br>44 5<br>44 5<br>45 5<br>46 5 |     |        | 4.0    | 7:0, 7:0    |
| 36         36         66, be           5.5         3.6         1.6, ne, ne,           5.5         6.6         3.6, se,           3         1.6         1.6, se,           3         1.6         1.6, se,           4         1.6, se,         1.6, se,           3         1.6         1.6, se,           4         1.6, se,         1.6, se,           7         1.6         1.6, se,           4.6         1.6, se,         1.6, se,           4.6         1.6, se,         1.6, se,   | 7 38 30 60, 60, 60<br>55 30 10, 10, 10<br>7 55 00 80, 80,<br>7 40 40 115, 83<br>7 40 40 105, 8<br>7 40 30 45<br>40 00 50   | 1   | 3.0    | 3.0    | 10.0        |
| 4 5.5 3.0 he me,<br>7 55 00 80, 80, 80,<br>3 4.0 4.0 hs, 80<br>7 4.0 4.0 hs, 80<br>7 4.0 4.0 hs, 80<br>4.0 4.0 4.5<br>4.0 0.0 5.0  | 4 55 50 He He He<br>55 00 80 80 80<br>9 4-0 He H5 23<br>1 4-0 He H5 23<br>1 4-0 40 45<br>4-0 30 45   | Y   | 3.0    | 3.0    | 6.0, 6.0    |
| 7 5.5 0.0 De, Pe,<br>9 4.0 4.0 113, 8.0<br>1 4.0 4.0 10,5, 8<br>7 4.0 3.0 4.5<br>4.0 0.6 6.0   | 3         5.5         0.0         Be, ge,           3         4.0         4.0         105, ge,           1         4.0         4.0         105, ge,           2         4.0         3.0         4.5           4.0         3.0         4.5           4.0         3.0         4.5  |     | 5.5    | 3.0    | 11.0. 11.0. |
| 8 4.0 4.0 4.5, 80<br>7 4.0 4.0 10.5, 8<br>5 4.0 3.0 4.5<br>4.0 0.0 8.0   | 9 4.0 4.0 116, 80<br>7 4.0 4.0 10,5, 8<br>7 4.0 3.0 4.5<br>4.0 3.0 4.5   | 7   | 5.5    | 0.0    | 8.0, 8.0,   |
| 2 4.0 4.0 11.5, 8.0<br>7 4.0 4.0 10.5, 8<br>5 4.0 3.0 4.5<br>4.0 0.0 6.0   | 9 4.0 4.0 115, 20<br>7 4.0 4.0 10,5 8<br>7 4.0 3.0 4.5<br>4.0 0.0 6.0  |     |        |        |             |
| 7 4.0 4.0 105, 8<br>6 4.0 3.0 4.5<br>4.0 0.0 6.0   | 7 4.0 4.0 10.5, 8<br>5 4.0 3.0 4.5<br>4.0 are 6.0  | 2   | 4.0    | 4.0    | 11.5, 8.0   |
| t 4.0 3.0 4.5<br>4.0 0.0 6.0   | e 4.0 3.0 4.5<br>4.0 0.0 6.0   | 2   | 4.0    | 4.0    | 10.5 8.     |
| 1 4.0 0.0 6.9  | 4.0 0.0 6.0  | e.  |        |        | 4.5         |
|  |  |     |        |        |             |
|  |  |     |        |        |             |
|  |  |     |        |        |             |
|  |  |     |        |        |             |

http://www.biostat.mcgill.ca/hanley/galton/





# "Transmuting" of Female Heights



Heights (in inches) of adult children in relation to their mid-parent height. (a) each daughter's height 'as is' (b) daughter's height multiplied by 1.08 (c) 5.2 inches added to daughter's height. Daughters' heights are shown in pink, and sons' in blue, symbols. Ellipses (75%) are drawn based on the observed means and covariances.

In all three panels, and in analyses for "Do Residuals Segregate along Family Lines?", the mid-parent height is calculated as (father's height + 1.08 x mother's height) / 2.

[Average Residual, in inches]

# STATISTICAL PRACTICE

# LA PRATIQUE DE LA STATISTIQUE

- · Be professional
- Communicate well
- Don't be dazzled by big data/money
- Think for yourself
- Put thinking before techniques

- Être professionnel
- Bien communiquer
- Ne pas être ébloui par les mégadonnées/l'argent
- Penser par soi-même
- Mettre la réflexion avant les techniques



# http://www.biostat.mcgill.ca/hanley → Publications, Presentations, Interviews, etc.

